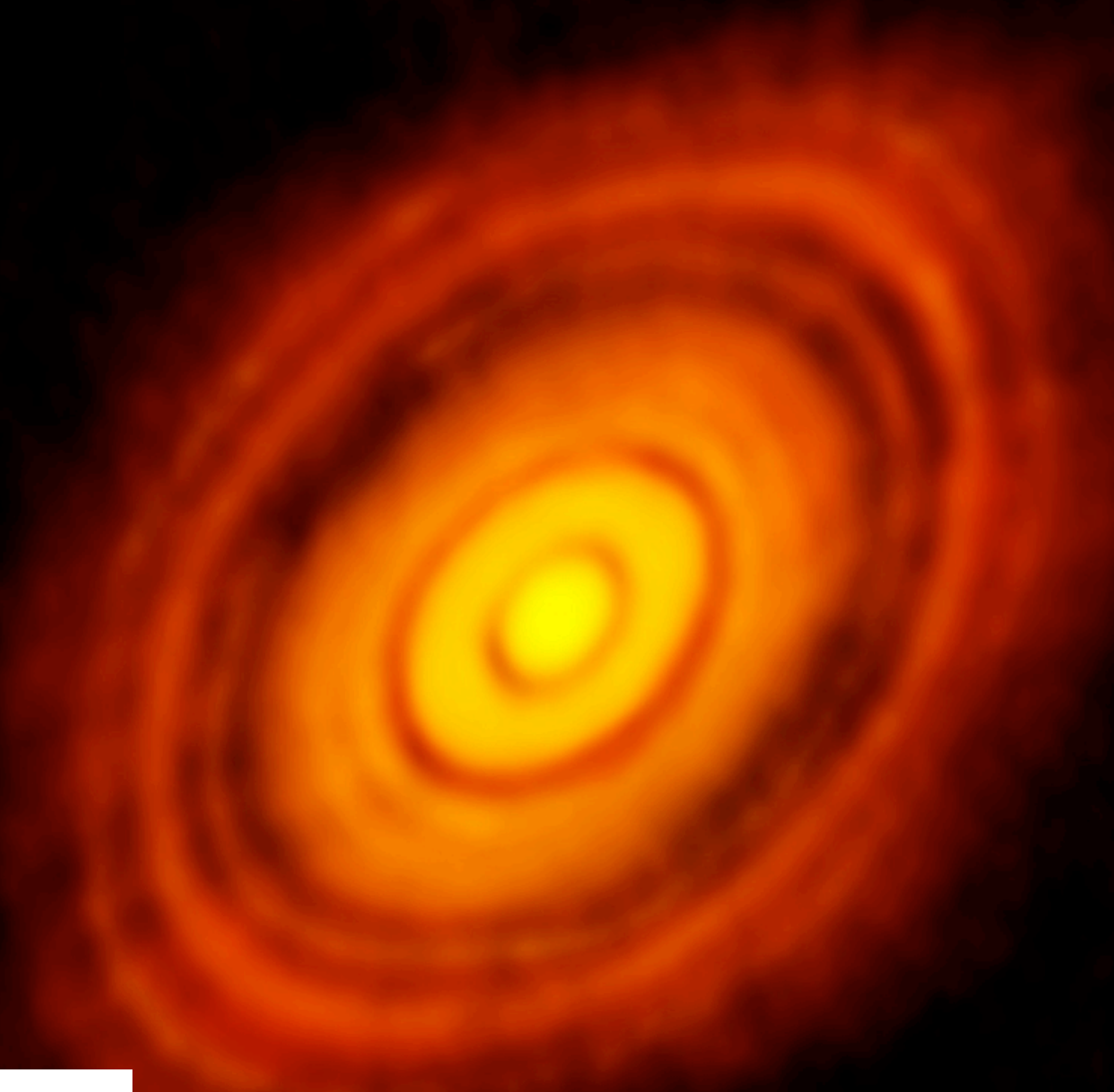


Formation of Planetary Systems

Lecture 2 - Protoplanetary discs

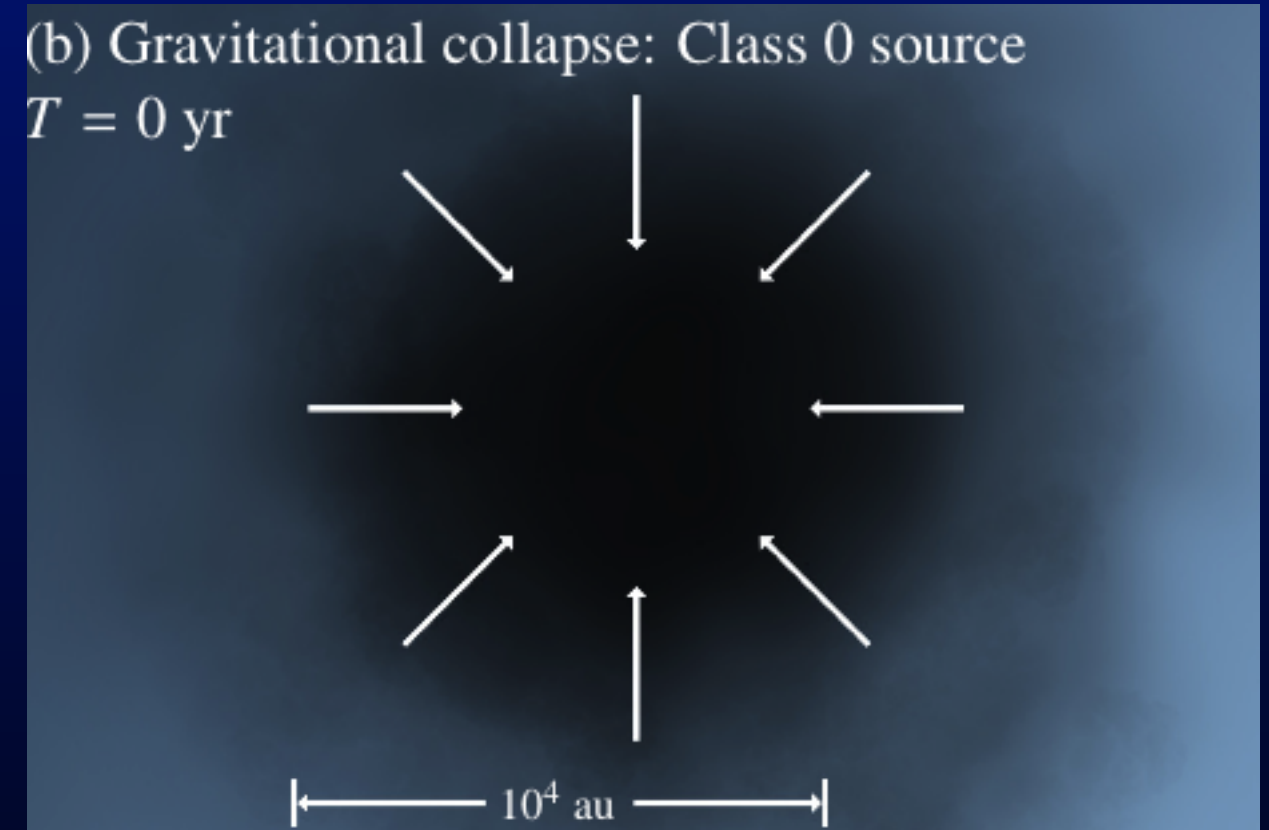
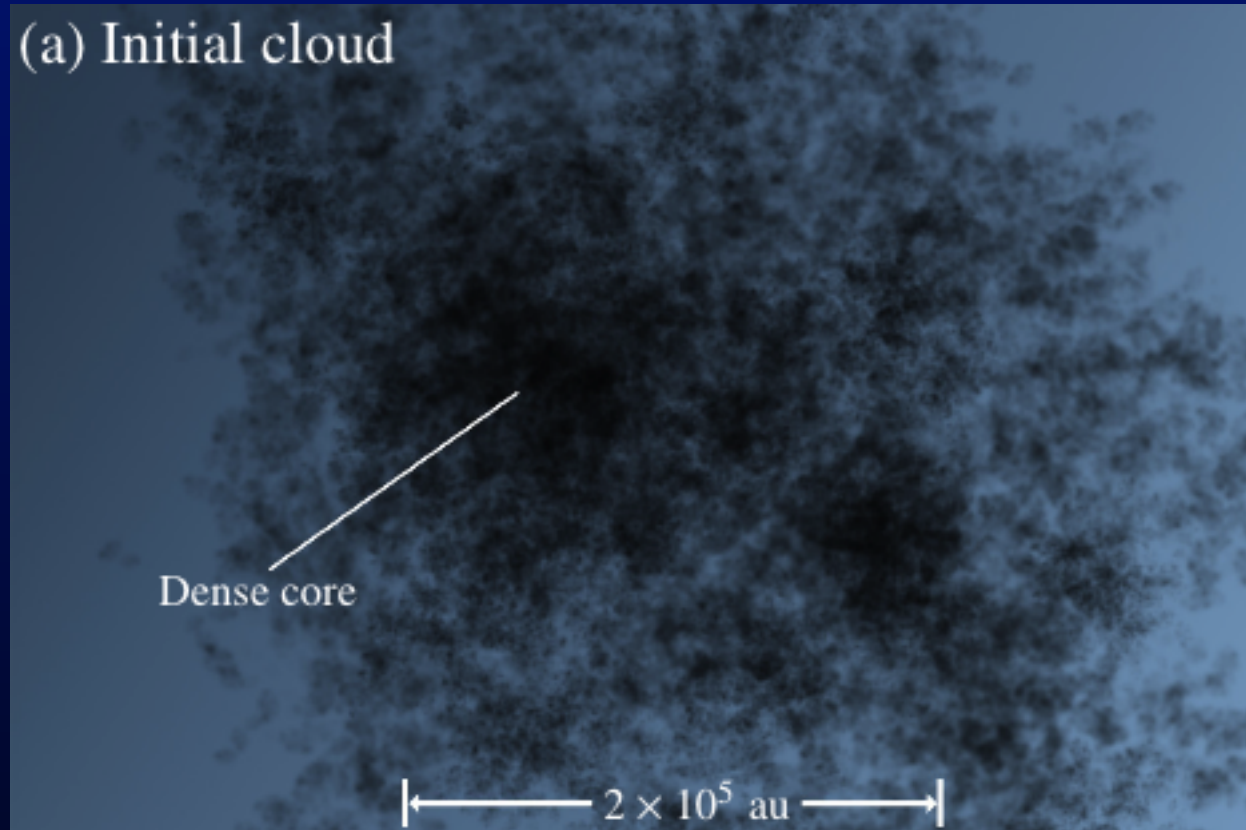


Course Outline

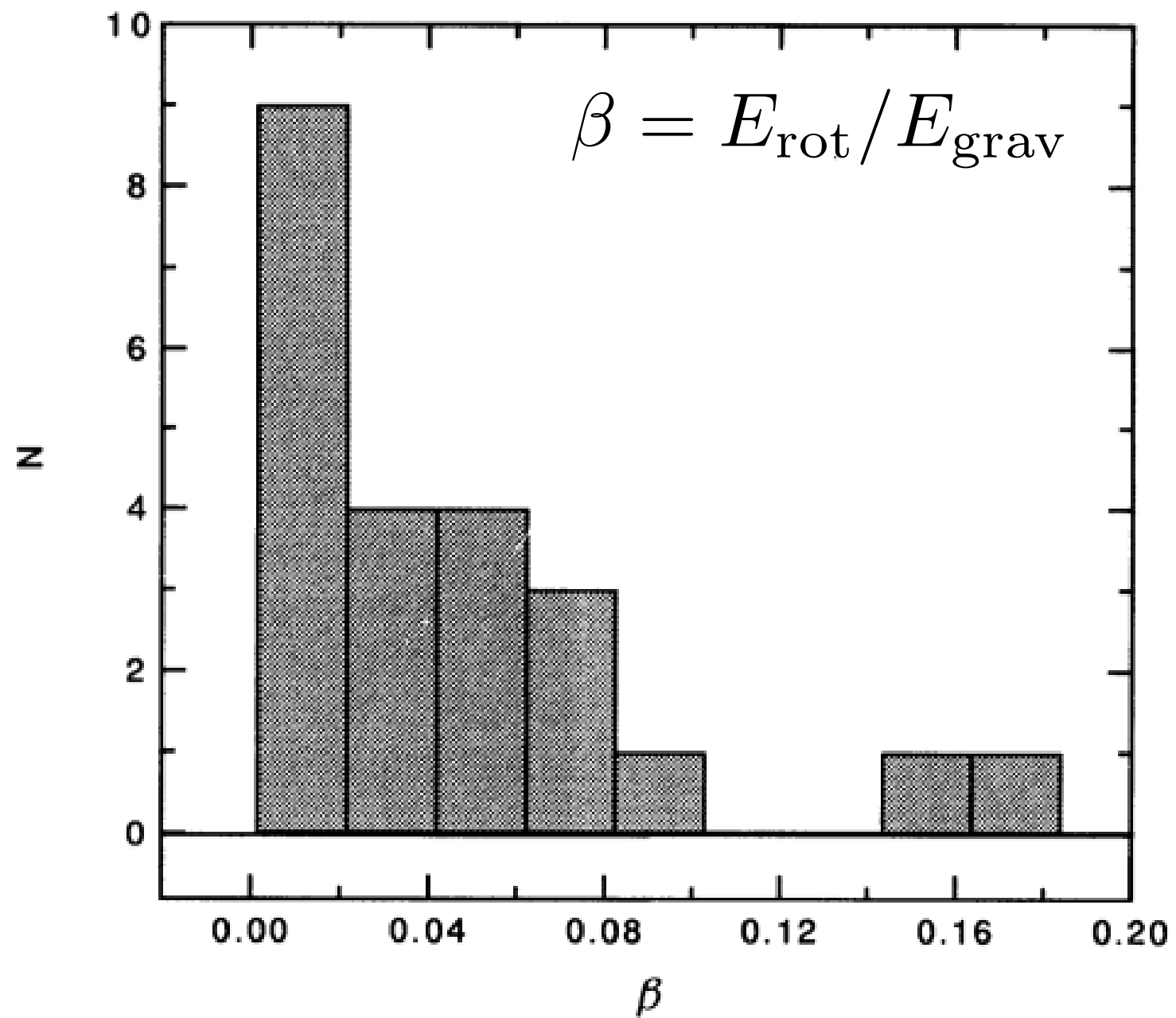
- 5 Lectures, 2 hours each (with a break in the middle!).
 - 1) Observations of planetary systems
 - 2) Protoplanetary discs
 - 3) Dust dynamics & planetesimal formation
 - 4) Planet formation
 - 5) Planetary dynamics
- Notes for each lecture will be placed on the course home page *in advance* - you may find it useful to annotate these as we go.
- These slides will also be posted online.
- Textbooks: Armitage - *Astrophysics of planet formation* (CUP).
Protostars & Planets series (V - 2007; VI - 2014)

Gravitational collapse

Figures from Alex Dunhill (PhD thesis, 2013), after Shu et al. (1987)



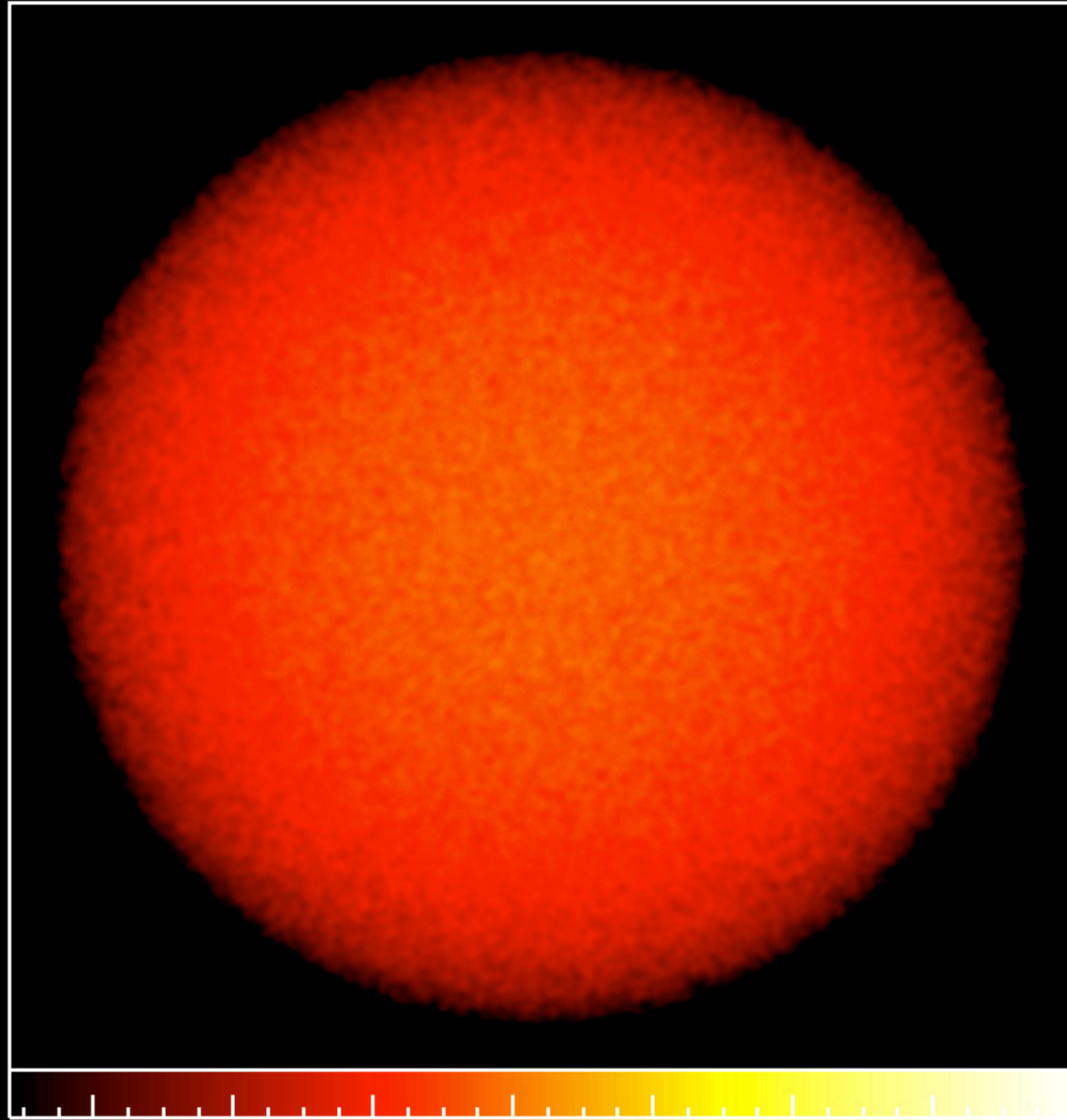
Measuring rotation



Goodman et al. (1993)

Dimensions: 82500. AU

Time: 0. yr



-1.4

-1.2

-1.0

-0.8

-0.6

-0.4

-0.2

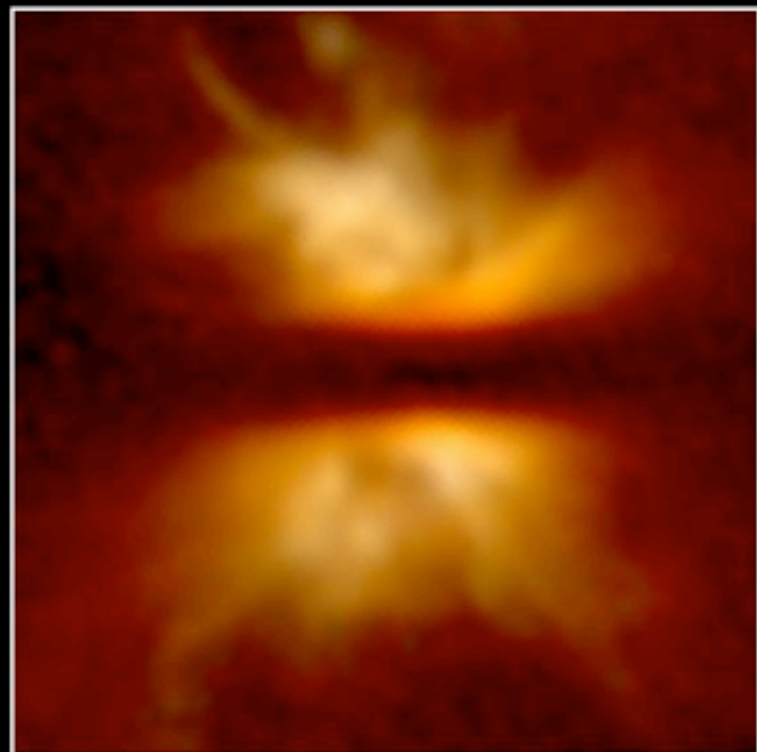
0.0

Log Column Density [g/cm^2]

Matthew Bate

Bate et al. (2002, 2003)

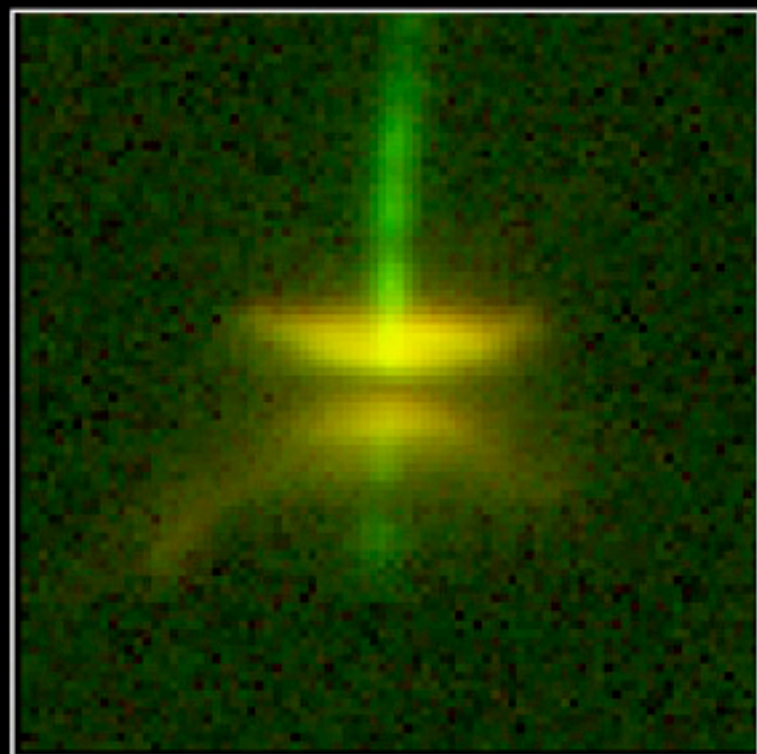
IRAS 04302+2247



Orion 114-426

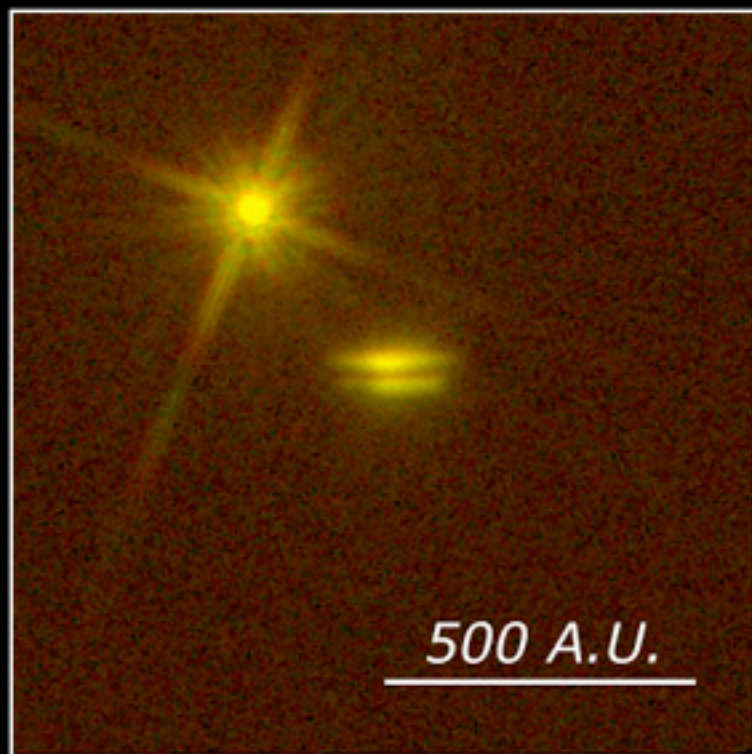


NICMOS

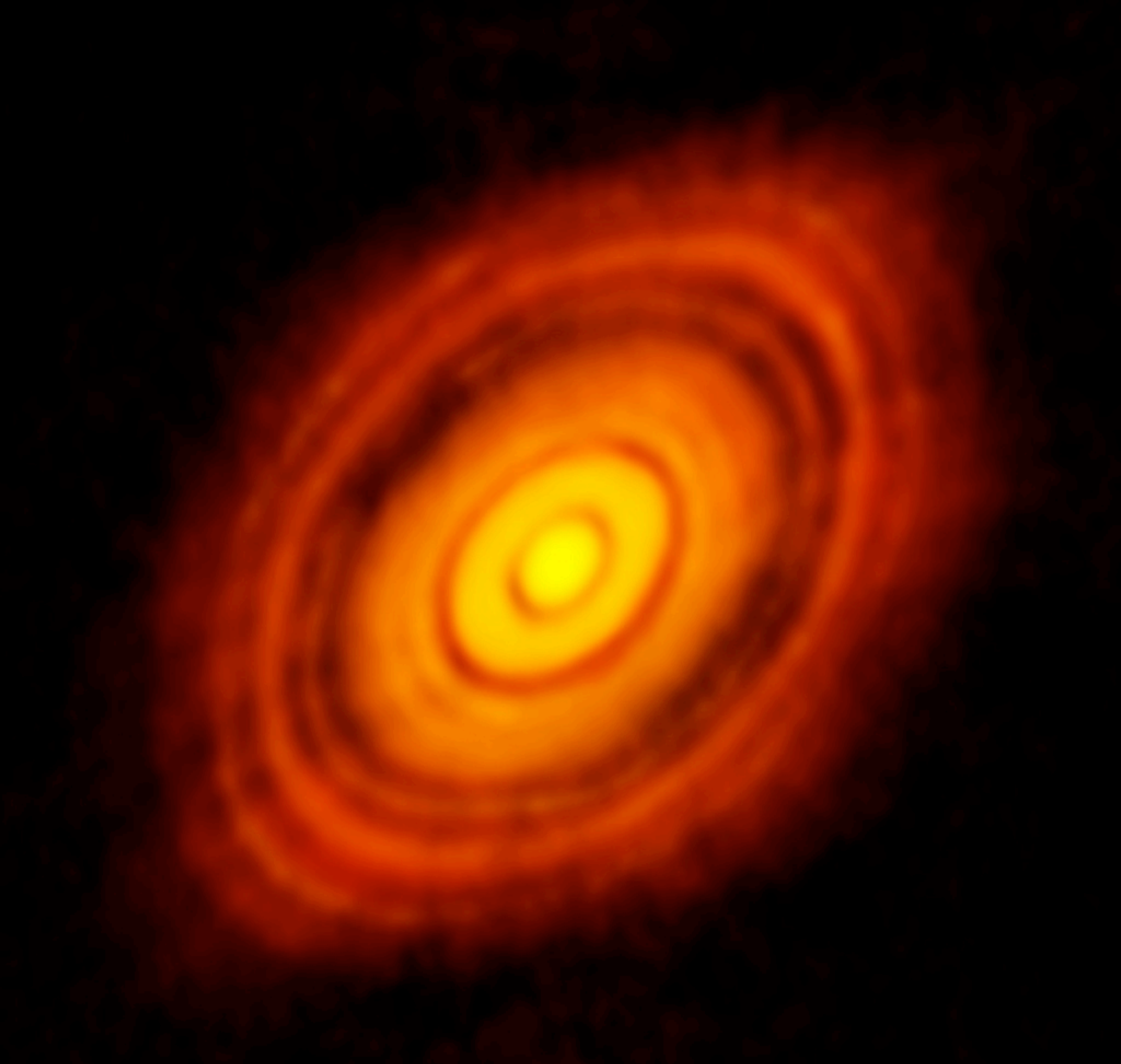


WFPC2

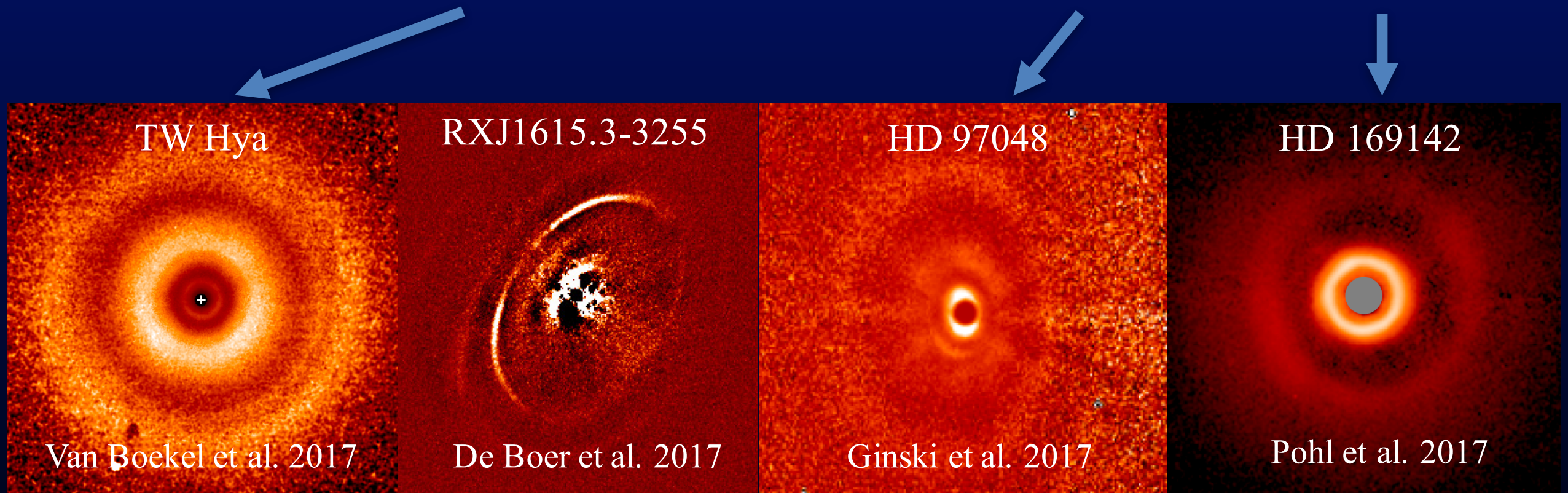
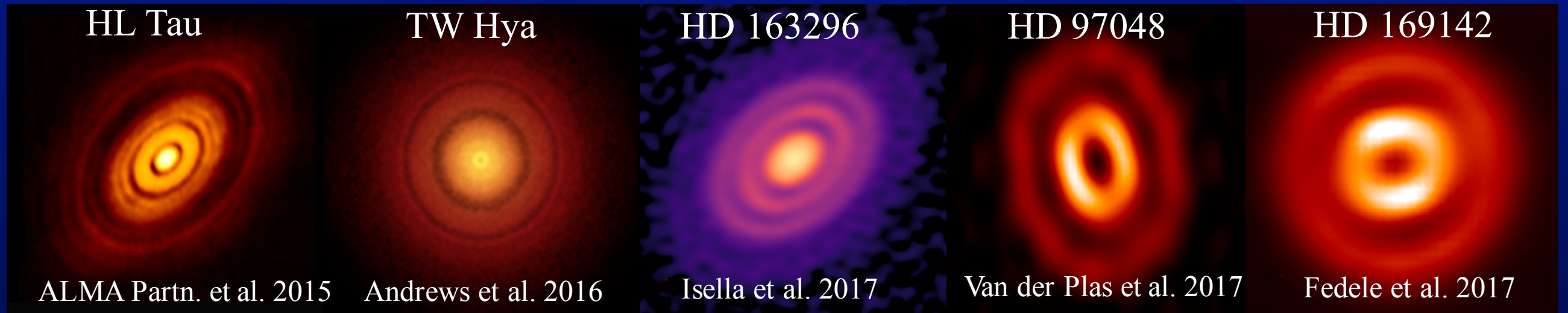
HH 30

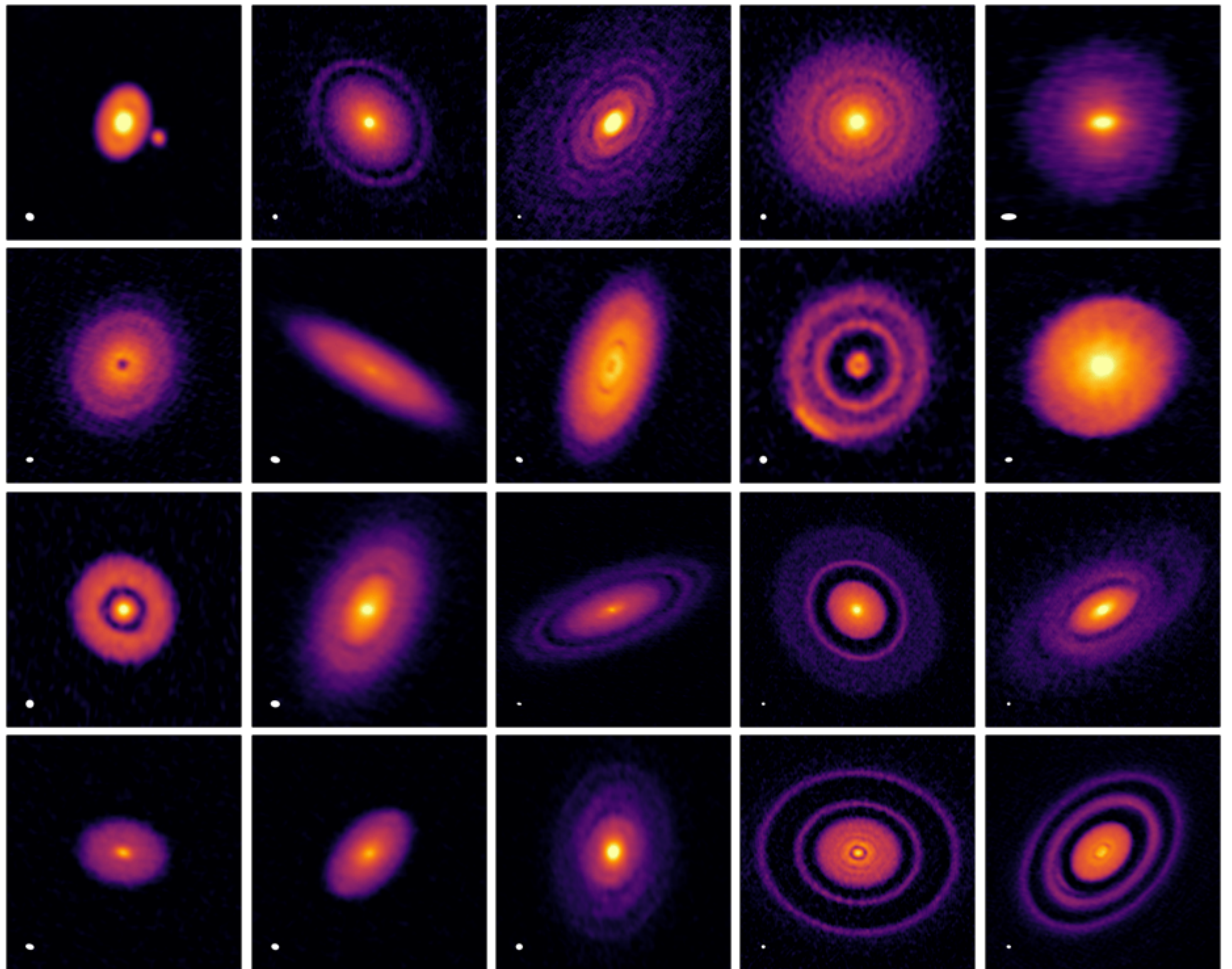


HK Tau/c



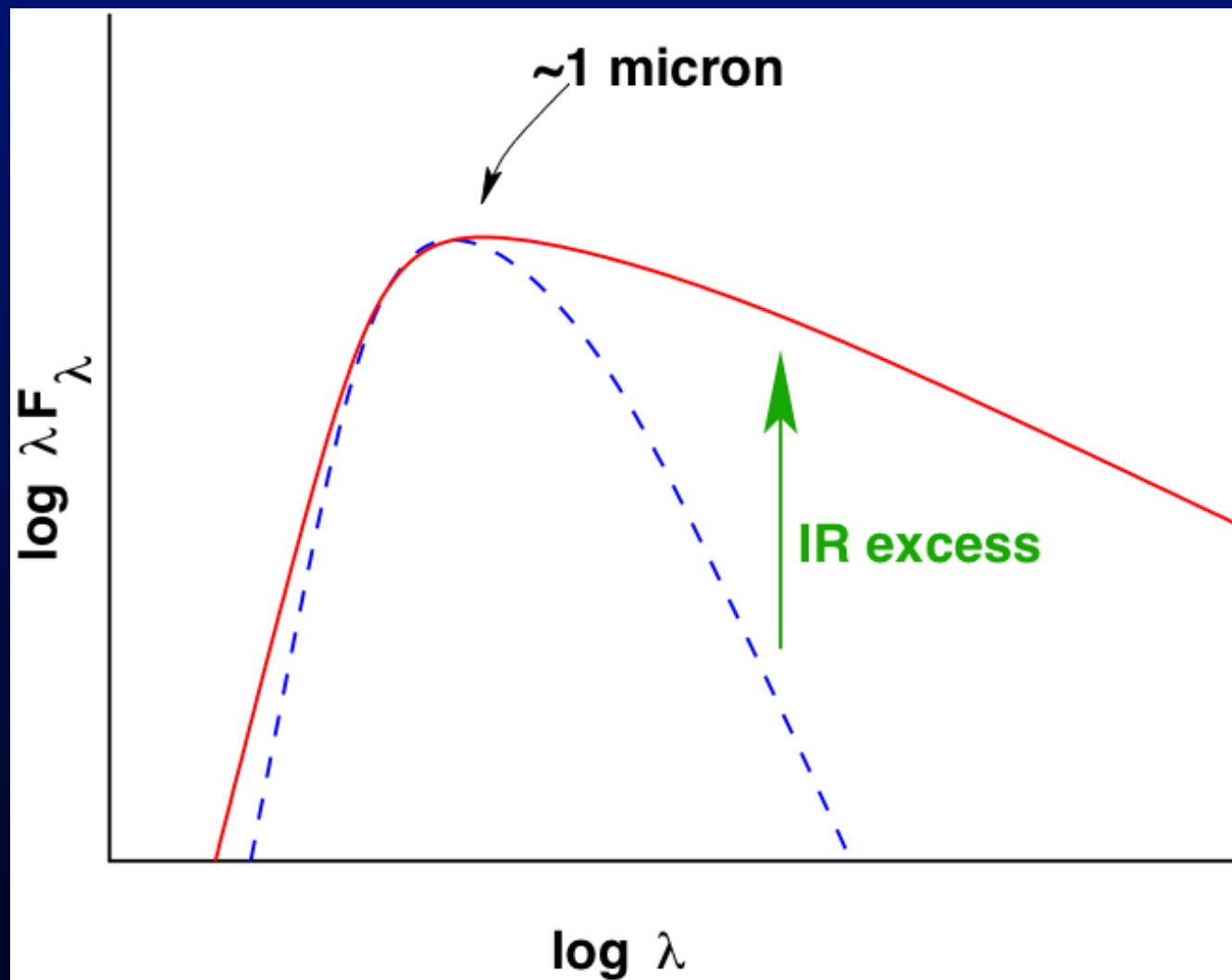
HL Tau @ 1.3mm: ALMA partnership (2015)





ALMA “DSHARP” survey; Andrews et al. (2018)

SED Classification Scheme

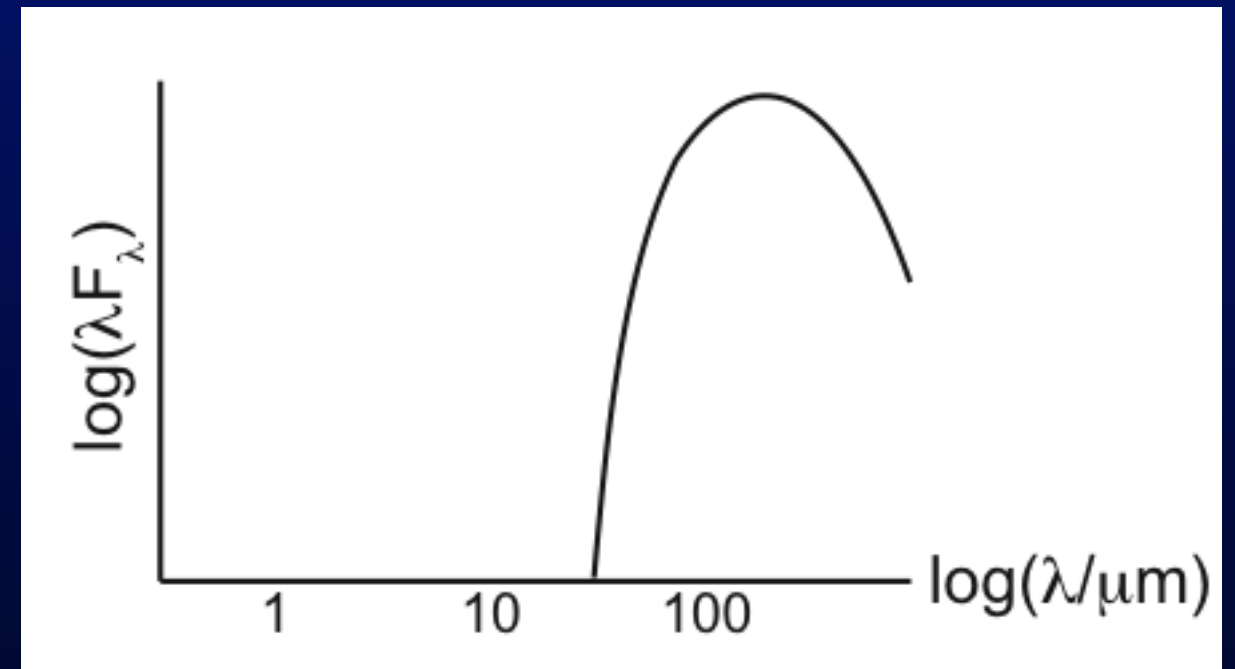
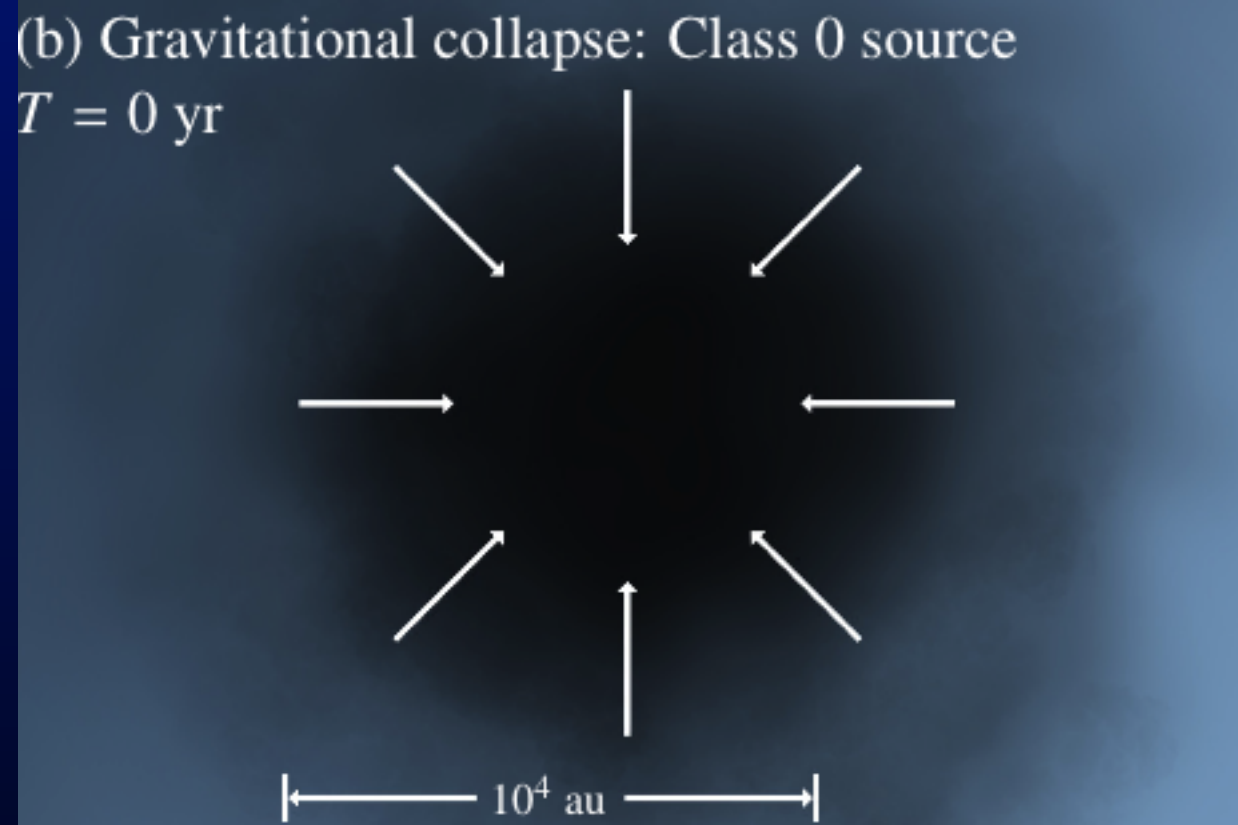


Armitage (2007)

$$\alpha_{\text{IR}} = \frac{d \log (\lambda F_\lambda)}{d \log \lambda}$$

SED Classification Scheme

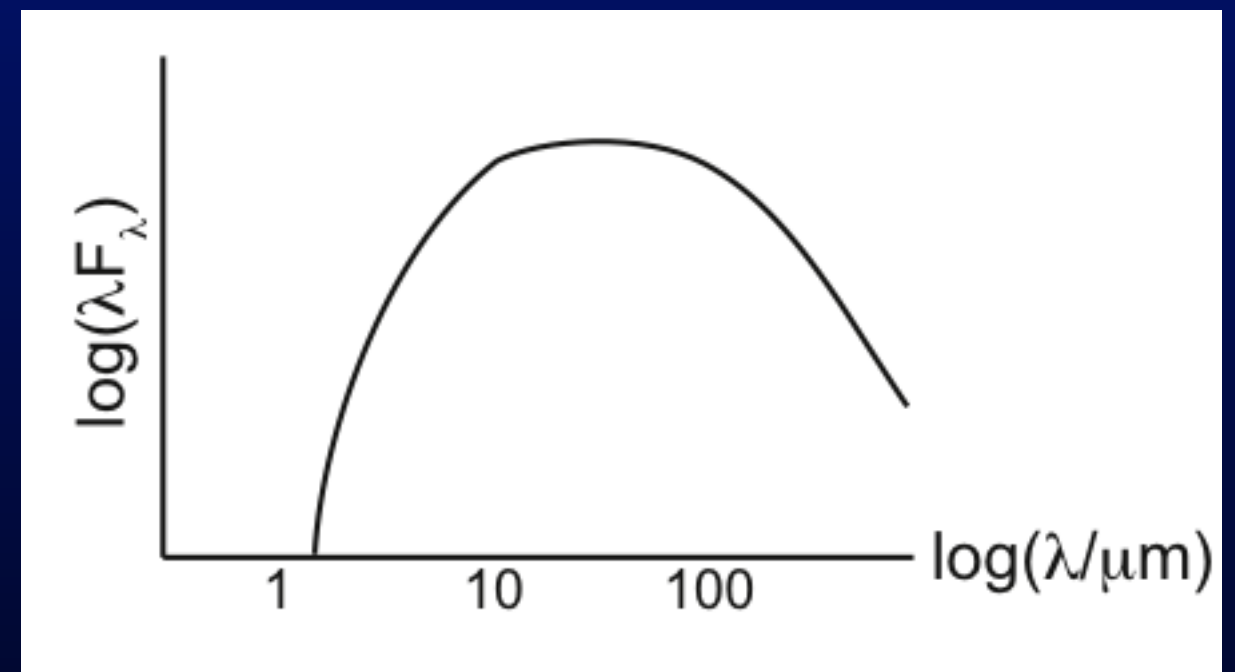
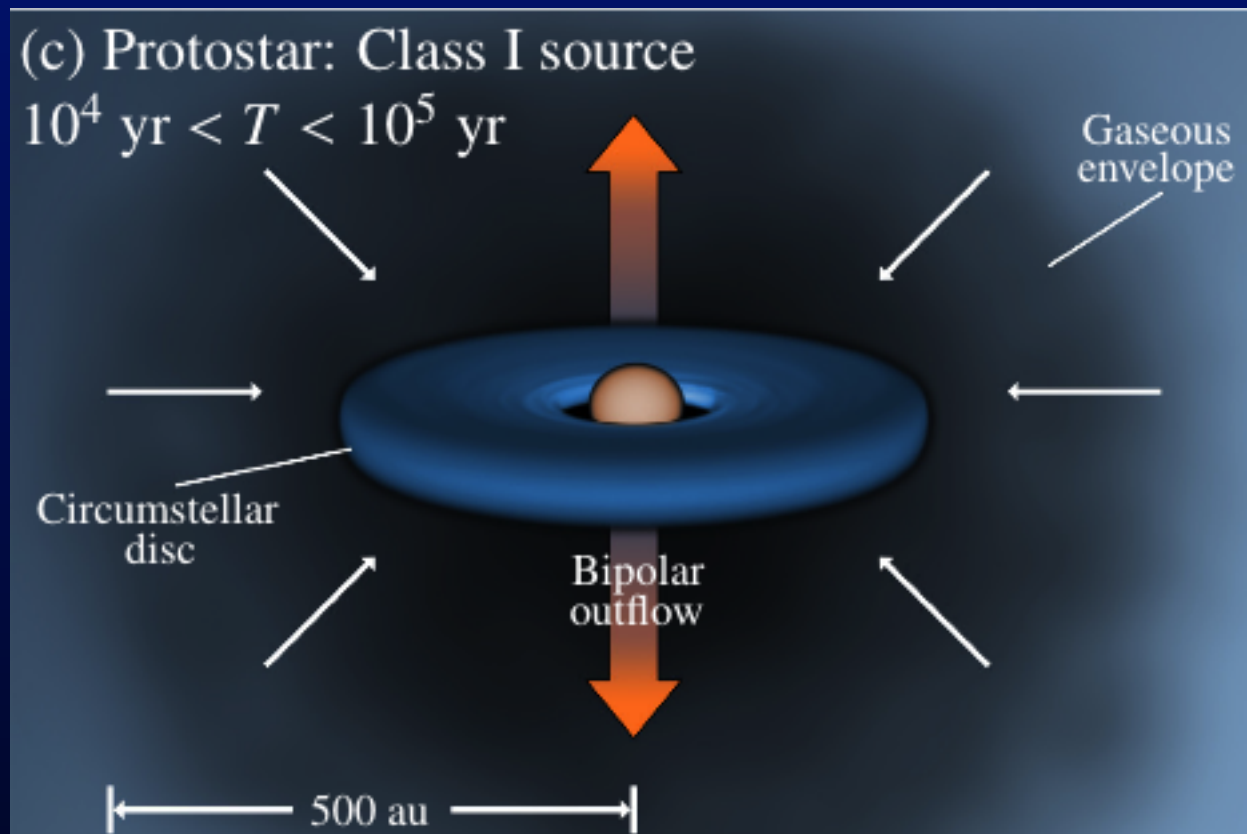
Figures from Alex Dunhill (PhD thesis, 2013) & Armitage (2010)



Class 0: sub-mm sources, no detectable IR emission

SED Classification Scheme

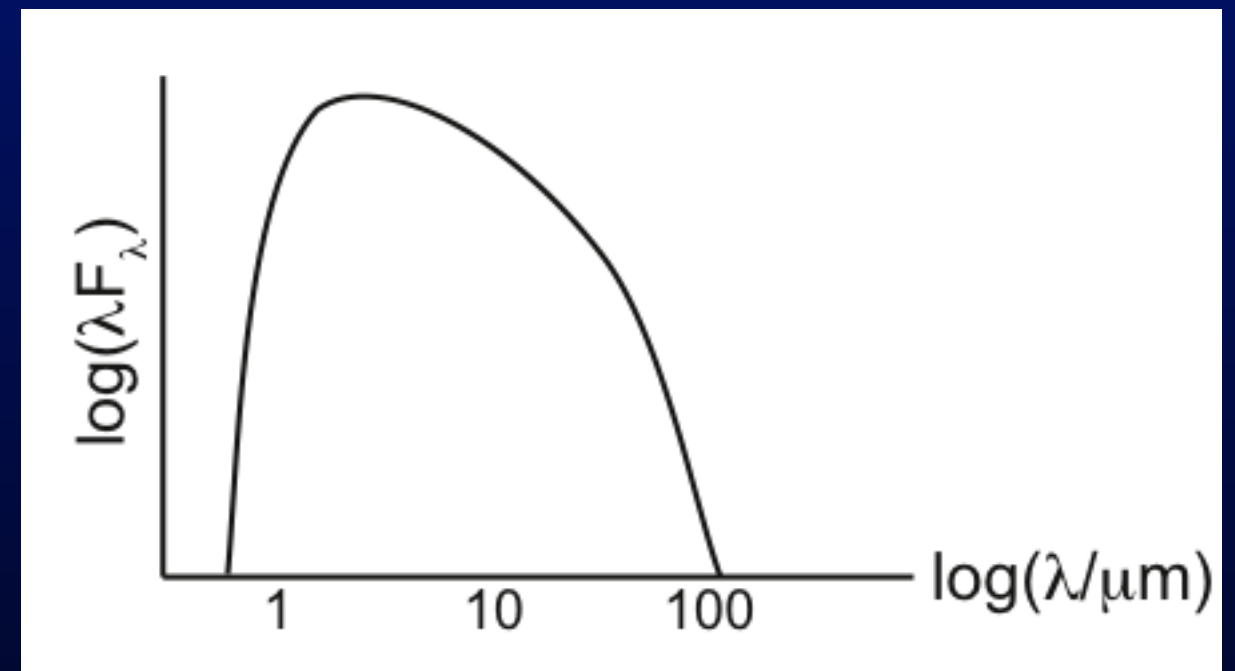
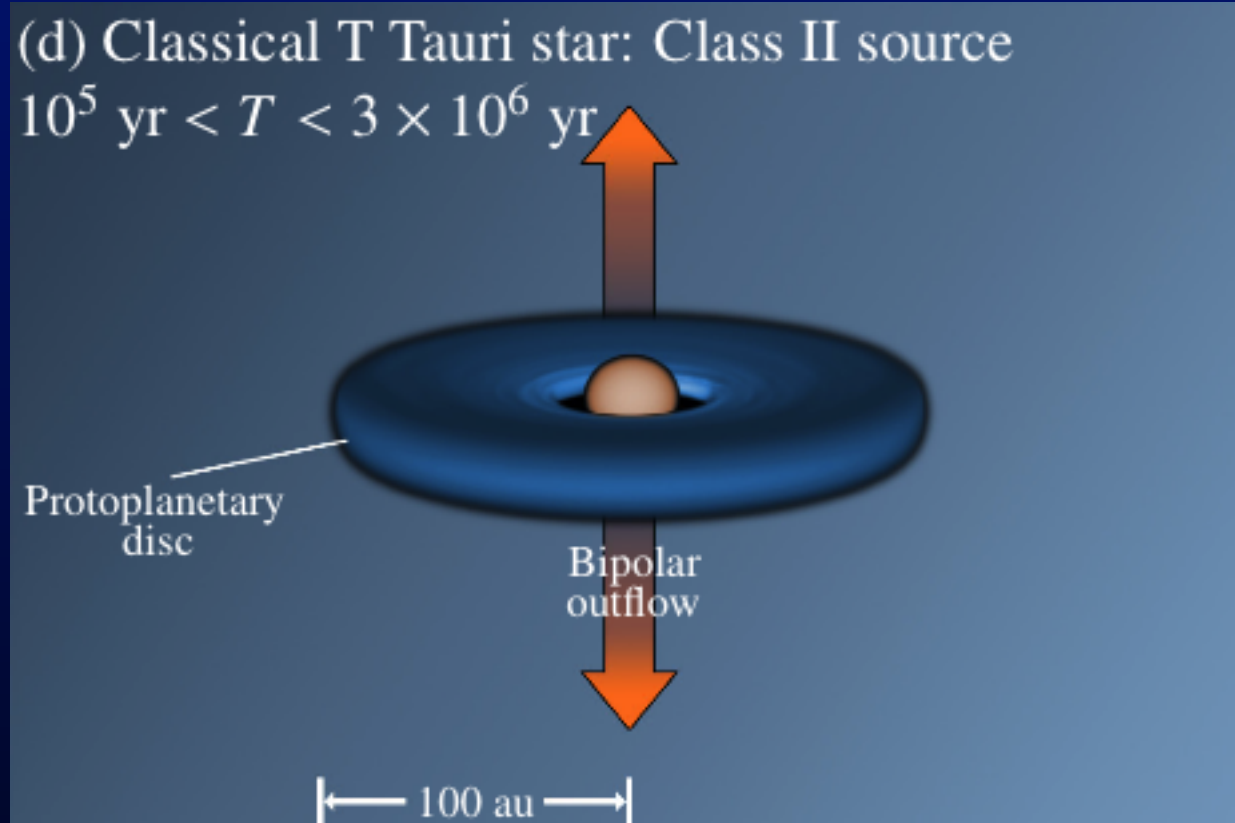
Figures from Alex Dunhill (PhD thesis, 2013) & Armitage (2010)



Class I: $\alpha_{\text{IR}} \gtrsim 0.0$

SED Classification Scheme

Figures from Alex Dunhill (PhD thesis, 2013) & Armitage (2010)

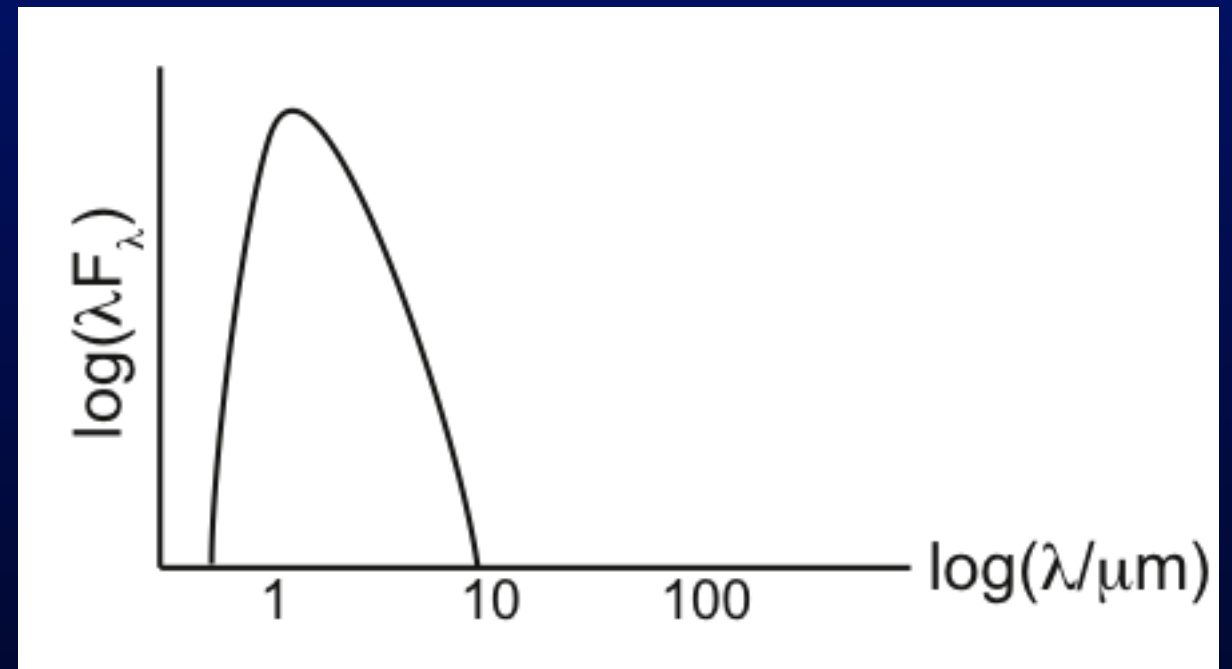
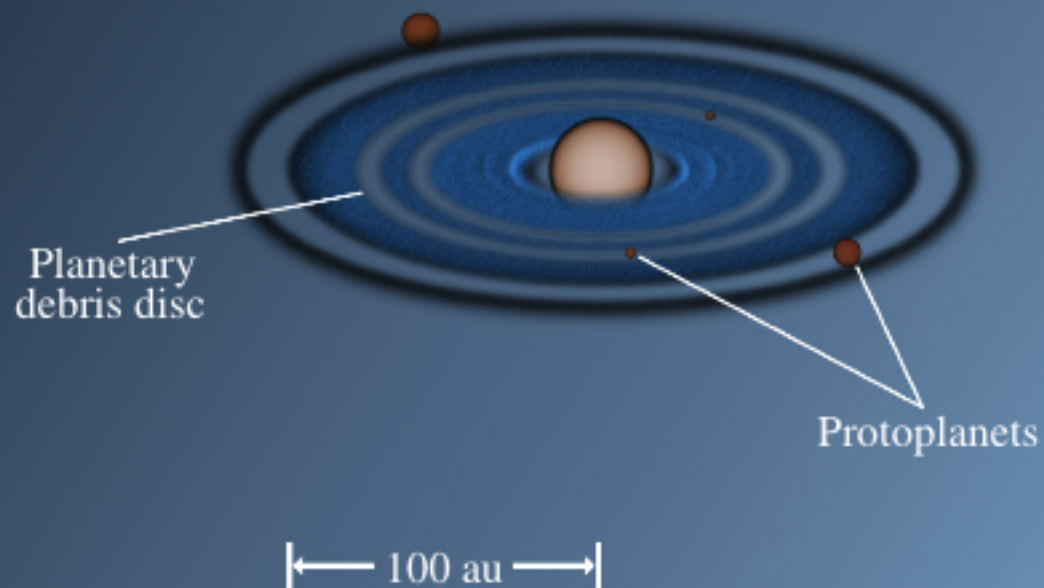


$$\text{Class II: } -1.5 \lesssim \alpha_{\text{IR}} \lesssim 0.0$$

SED Classification Scheme

Figures from Alex Dunhill (PhD thesis, 2013) & Armitage (2010)

(e) Weak-lined T Tauri star: Class III source
 $3 \times 10^5 \text{ yr} < T < 5 \times 10^7 \text{ yr}$

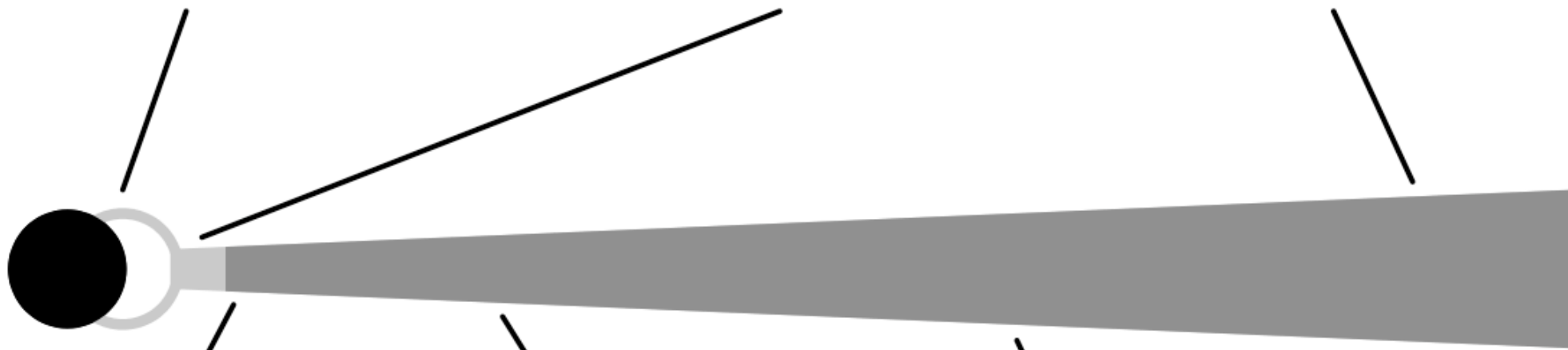


Class III: $\alpha_{\text{IR}} \sim -1.5$

Observations of protoplanetary discs

GAS

UV excess, veiling, broad emission lines
Hot gas emission lines CO (ro-vib), H₂, etc.
Cold gas emission lines CO (rotational), etc.



near-IR

mid-IR

far-IR

(sub)-mm

$\tau \gg 1$

$\tau \sim 1$

$\tau < 1$

0.1AU

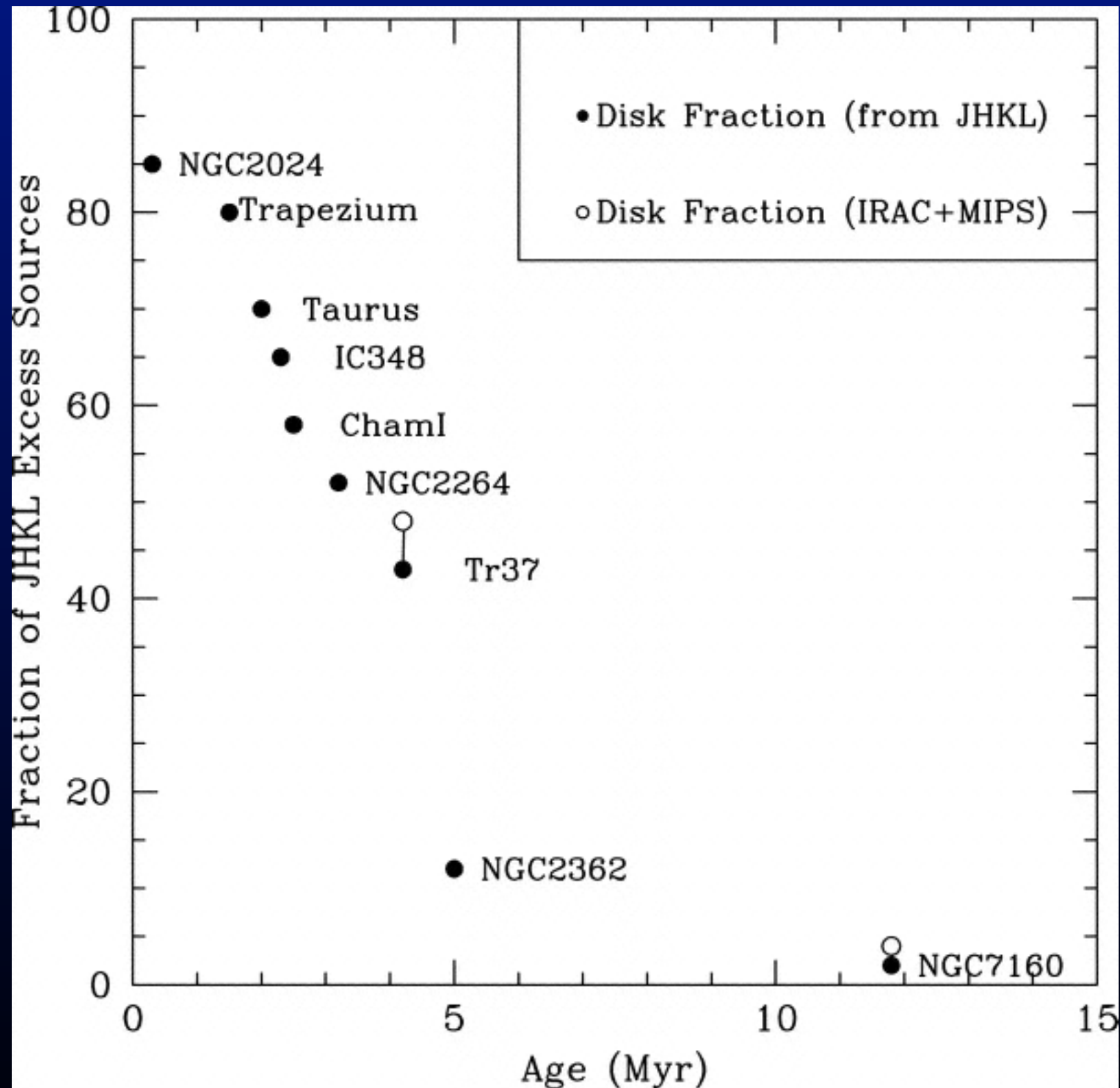
1AU

10AU

100AU

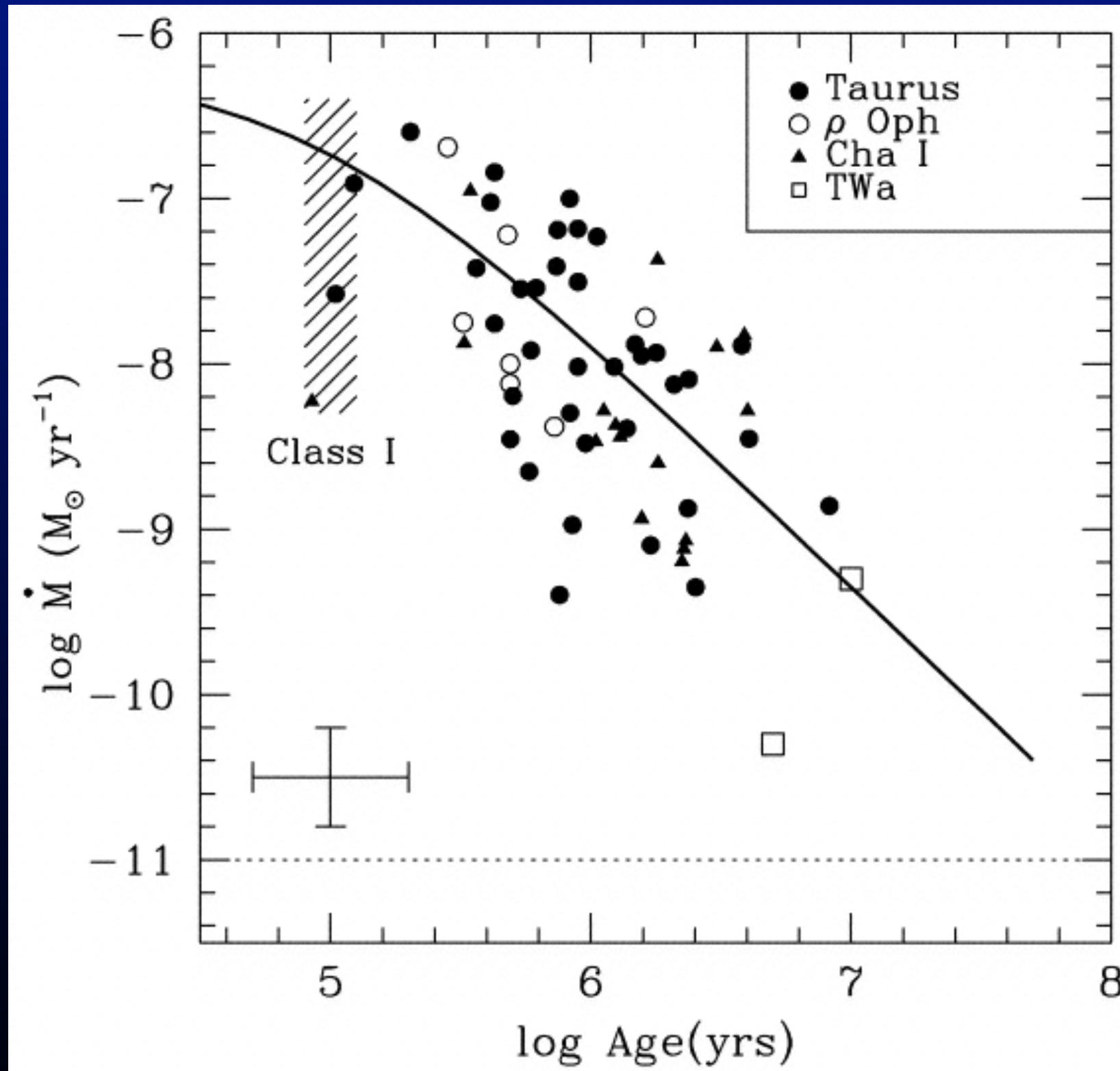
DUST

Disc lifetimes



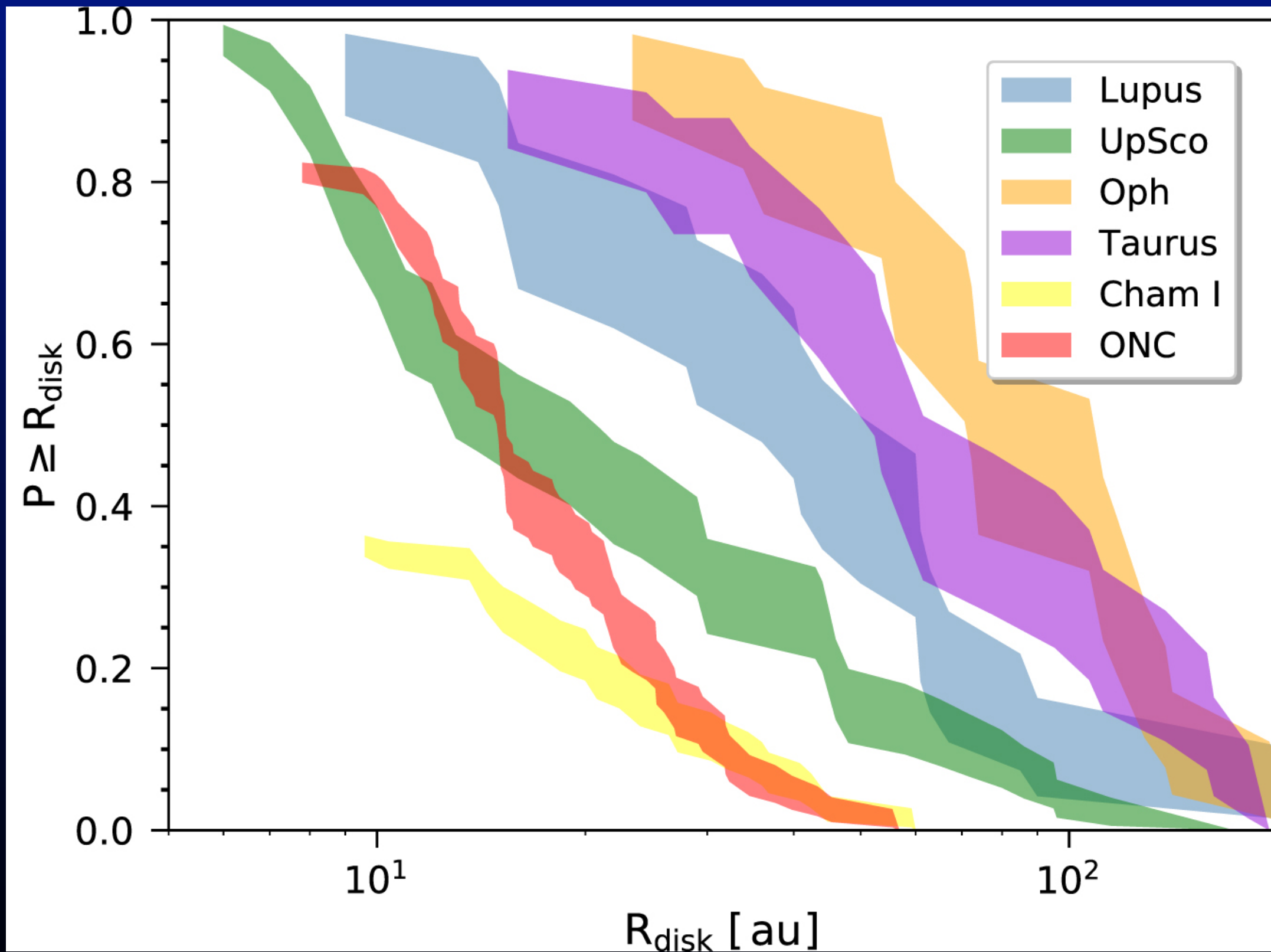
Sicilia-Aguilar et al. (2006)

Accretion rates



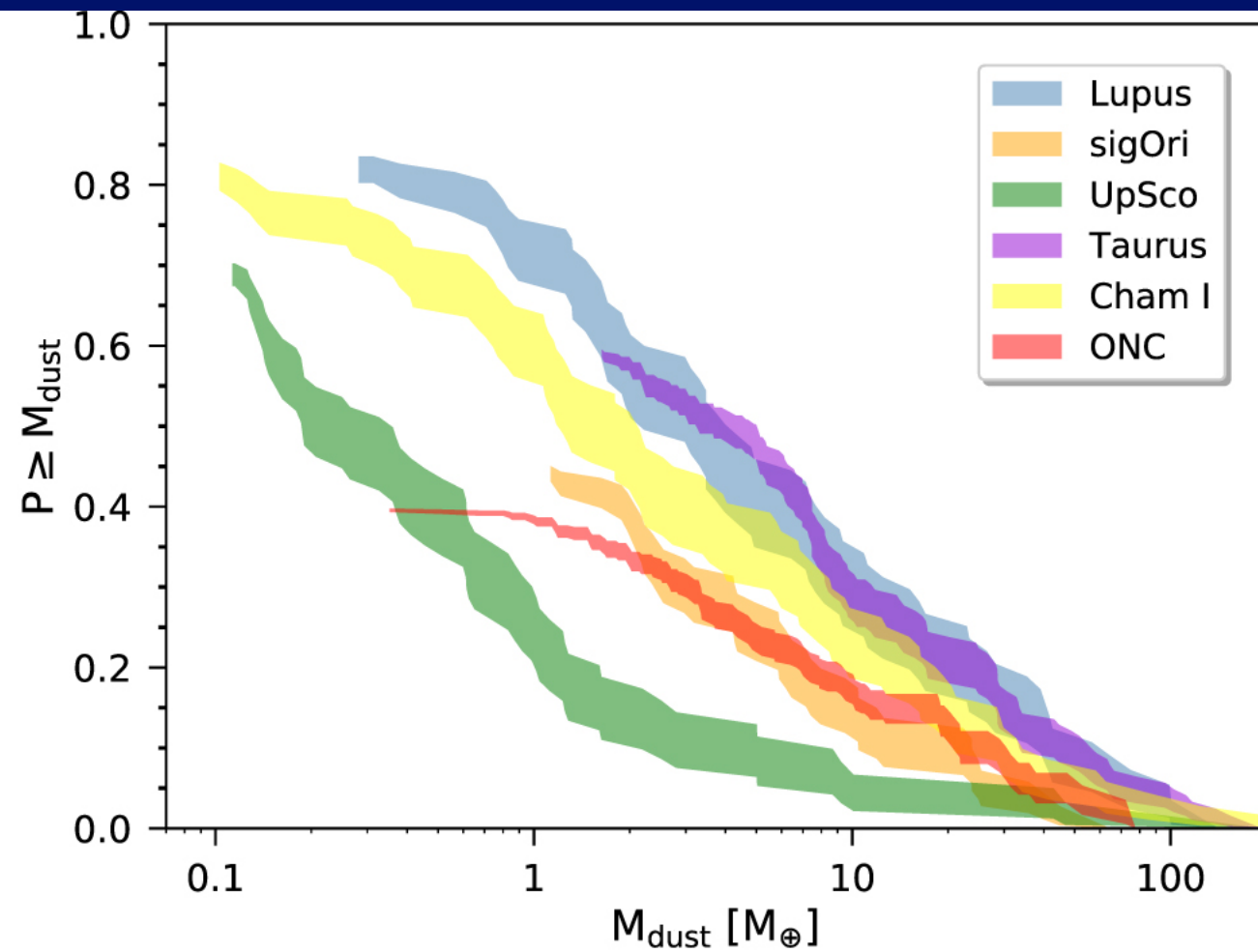
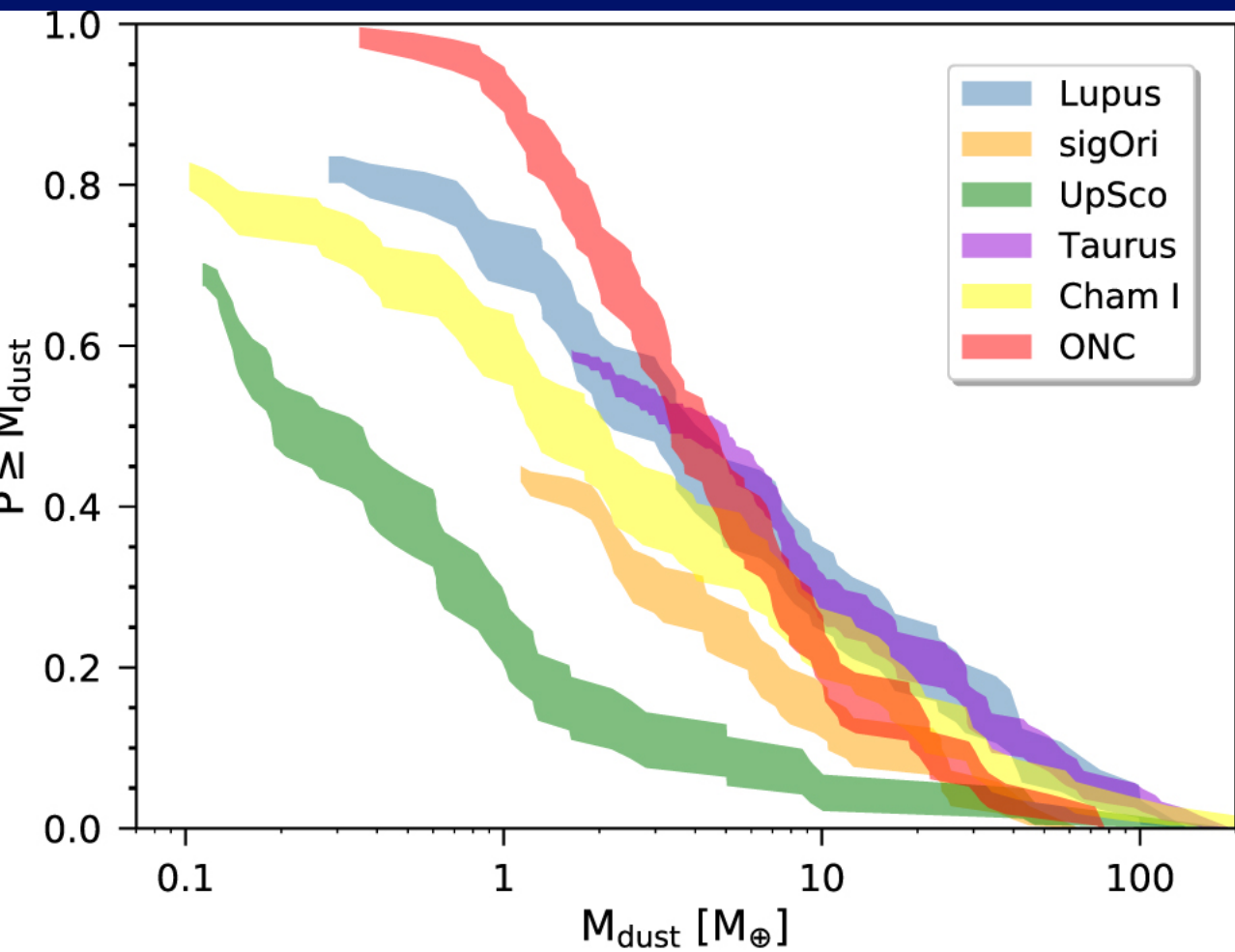
Muzerolle et al. (2000)

Disc sizes



Data compilation from Eisner et al. (2018)

Disc masses



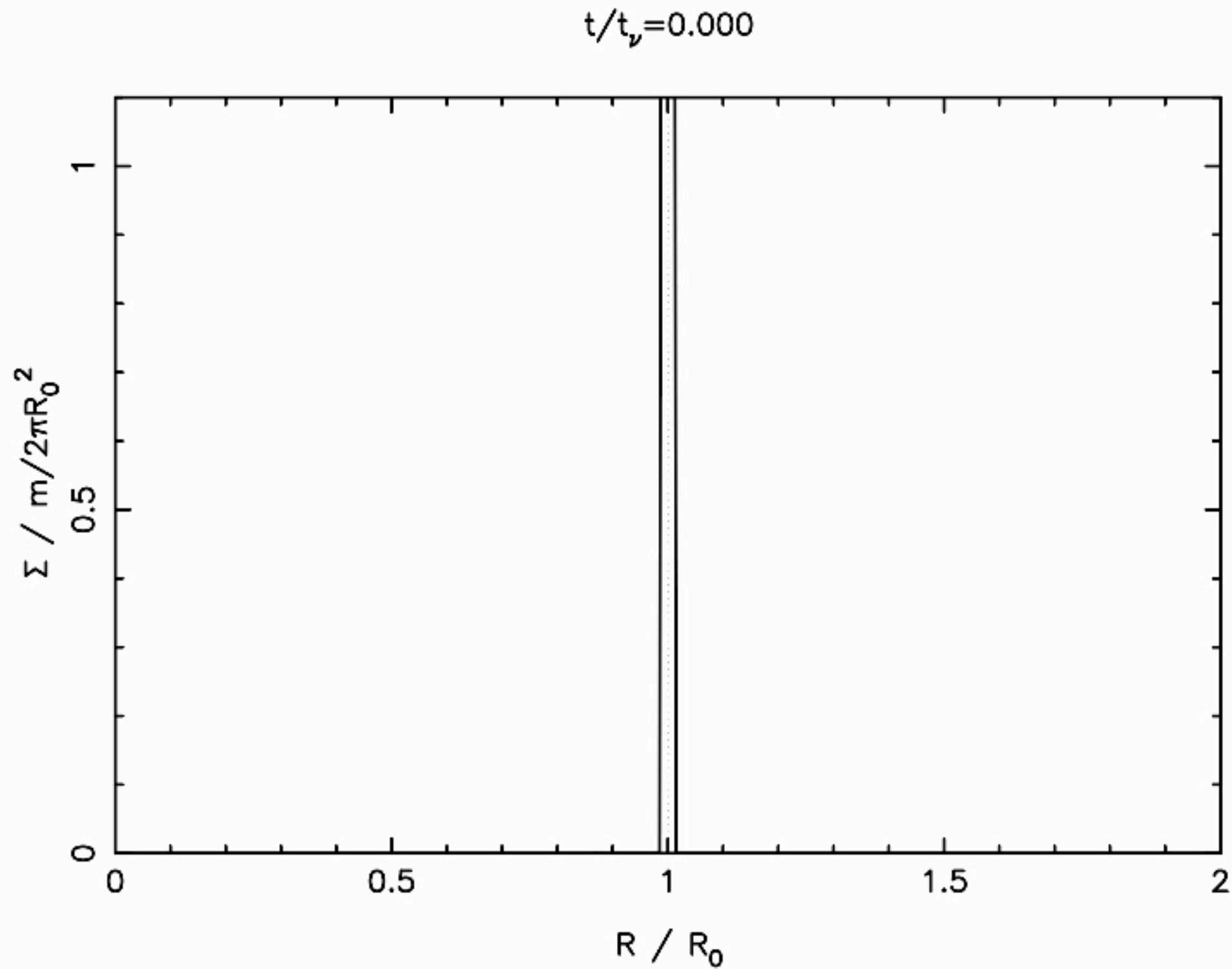
Data compilation from Eisner et al. (2018)

Observational Summary

- Discs are tens to hundreds of AU in size.
- Disc masses range from $>0.1 M_{\odot}$ to $\leq 0.001 M_{\odot}$.
- Accretion rates span $>10^{-7} M_{\odot} \text{yr}^{-1}$ to $\leq 10^{-10} M_{\odot} \text{yr}^{-1}$.
- Disc lifetimes are $\sim \text{Myr}$ (gas and dust tracers), with significant scatter.
- Cessation of (gas) accretion roughly simultaneous with (dust) disc clearing.
- Disc lifetimes set a limit on the time-scale for (giant) planet formation.
- Disc observations tell us the typical conditions for planet formation.

Viscous spreading ring

Pringle (1981)



Viscous disc similarity solution

Lynden-Bell & Pringle (1974)

$$\nu \propto R^\gamma$$

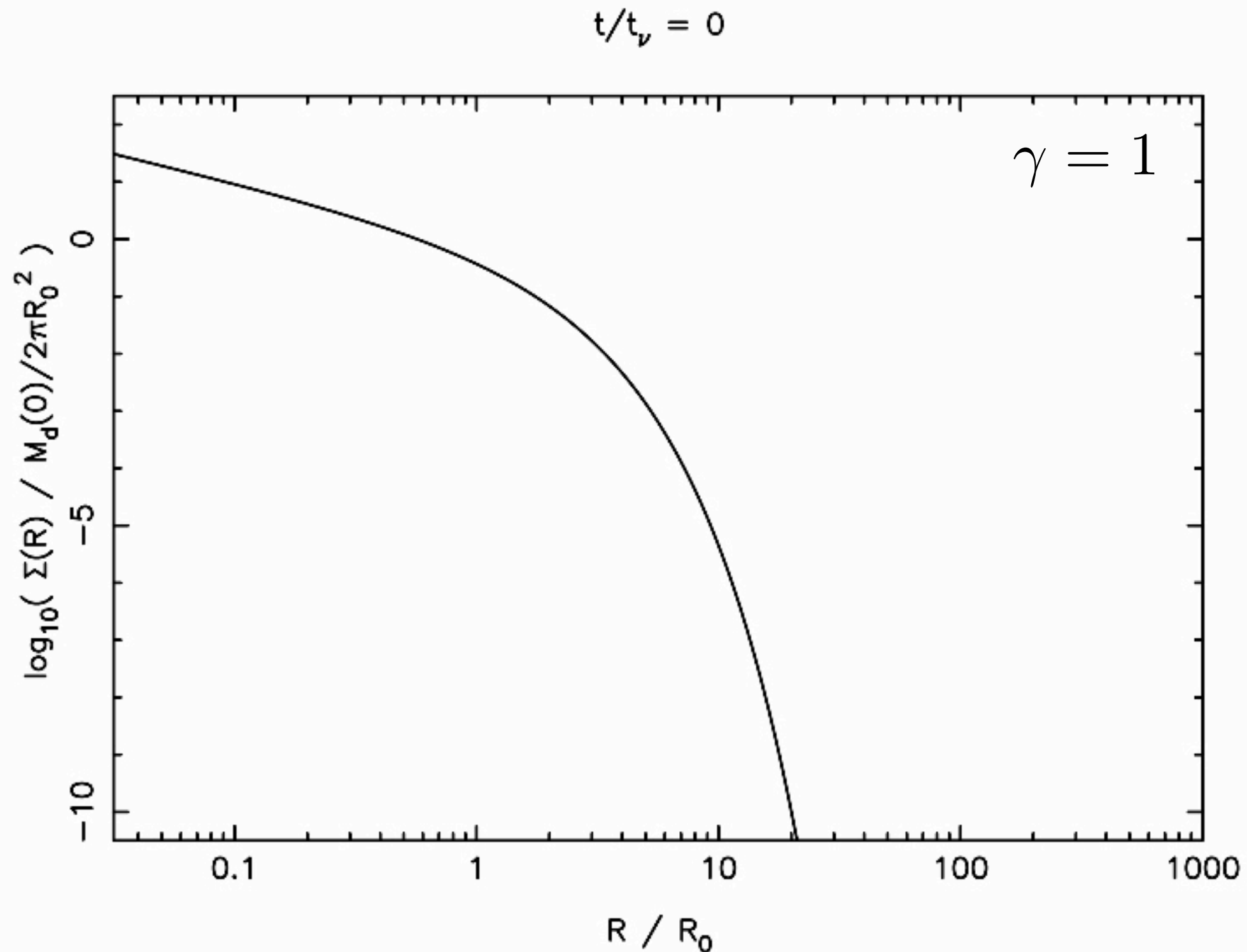
$$\Sigma(R, t) = \frac{M_d(0)(2 - \gamma)}{2\pi R_0^2 r^\gamma} \tau^{\frac{-(5/2 - \gamma)}{2 - \gamma}} \exp\left(-\frac{r^{2 - \gamma}}{\tau}\right)$$

$$r = R/R_0 \quad \tau = t/t_\nu + 1 \quad t_\nu = \frac{R_0^2}{3(2 - \gamma)^2 \nu_0}$$

$$\dot{M}_{acc} = \frac{M_d(0)}{2(2 - \gamma)t_\nu} \tau^{\frac{-(5/2 - \gamma)}{2 - \gamma}}$$

Viscous disc similarity solution

Lynden-Bell & Pringle (1974)



Disc stability criteria

- Purely hydrodynamic disc (Rayleigh). Unstable if:

$$\kappa^2 = \frac{2\Omega}{R} \frac{d}{dR} (R^2\Omega) < 0$$

- MHD disc. Unstable if:

$$(\mathbf{k} \cdot \mathbf{u}_A)^2 + \frac{d\Omega^2}{d \ln R} < 0$$

- Alfvén velocity:

$$u_A = \sqrt{B^2 / 4\pi\rho}$$

- In limit $B \rightarrow 0$ (weak B-field), unstable if:

$$\frac{d\Omega^2}{d \ln R} < 0$$

The magnetorotational instability

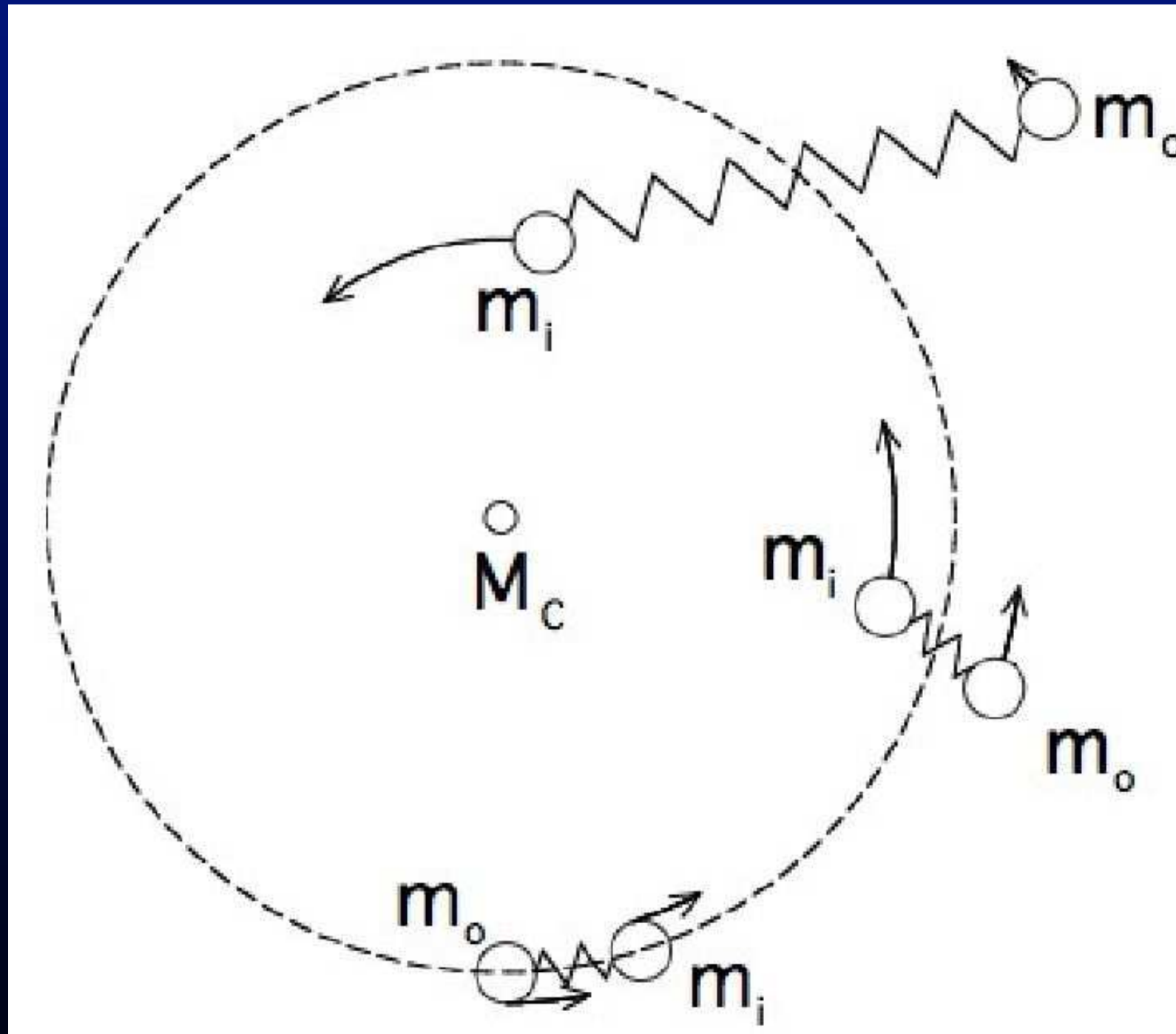
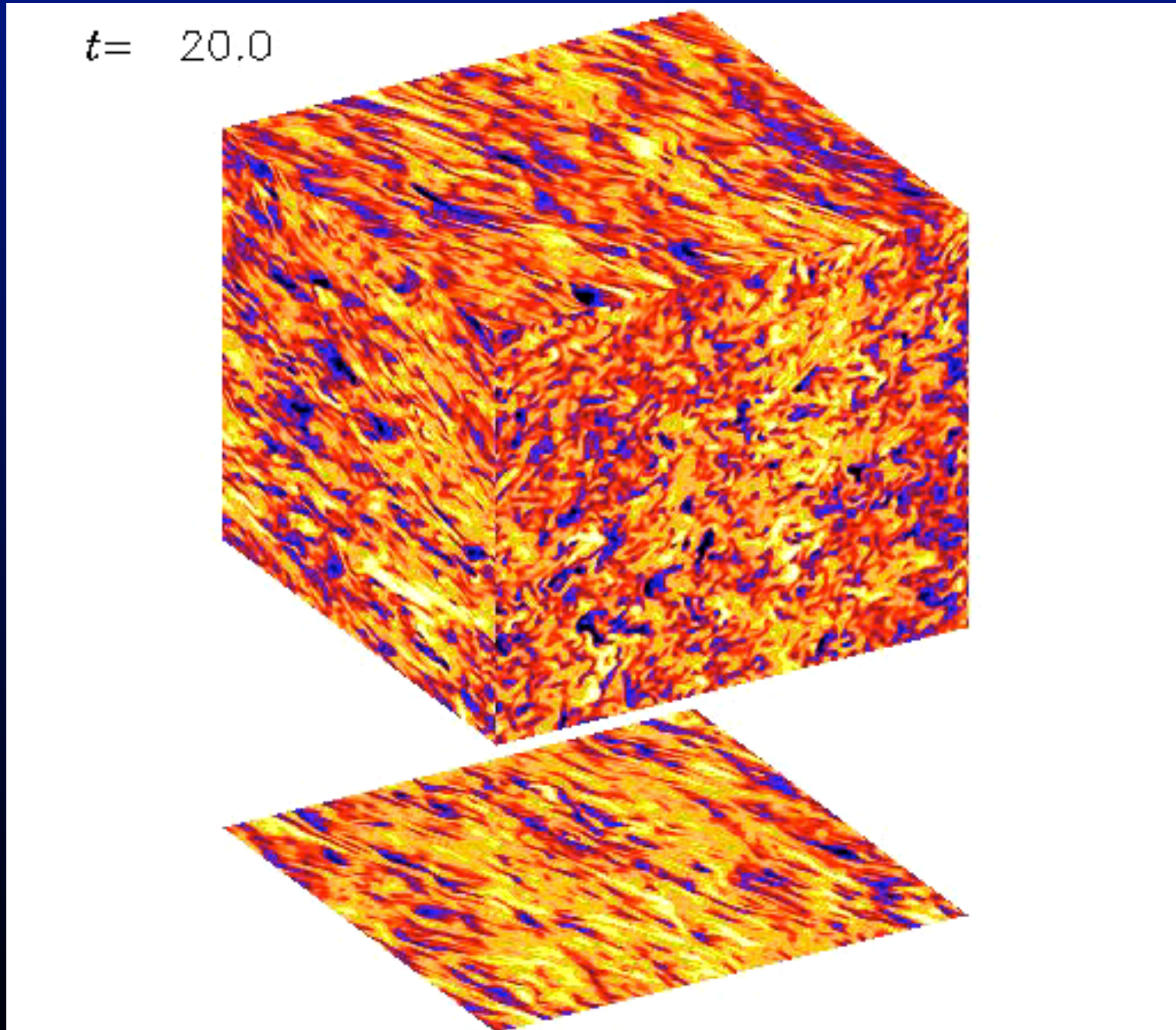


Figure from Balbus (2011)

Local simulations (ideal MHD)



Animation courtesy of Anders Johansen (Lund)

Global simulations (ideal MHD)

Accretion and Outflows in 3D Global MHD Simulations of Stratified Protoplanetary Disk

Mario Flock
Ringberg 2011

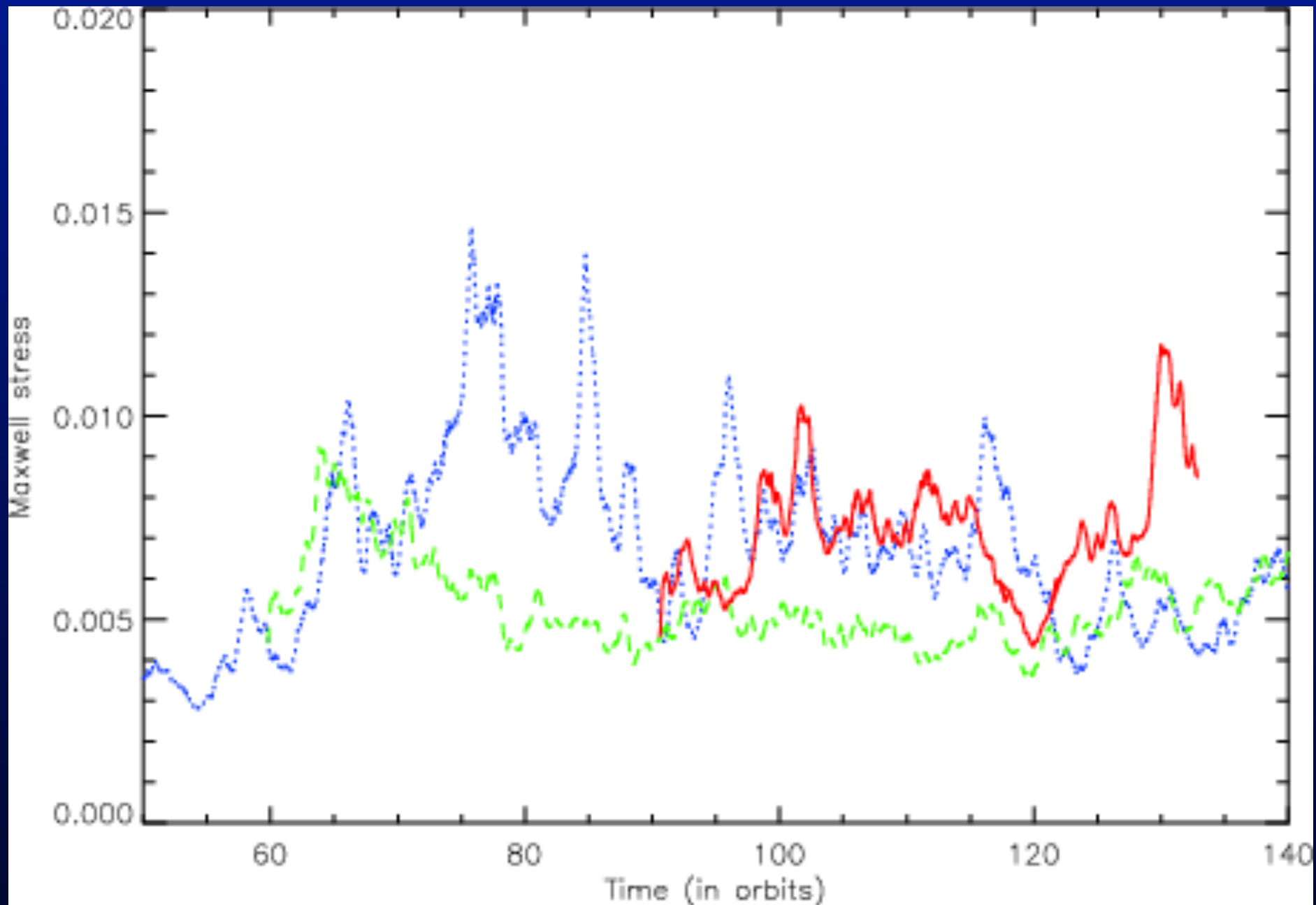


Figure from Fromang (2010)

Numerical simulations suggest that MRI turbulence can drive angular momentum transport with an “effective alpha” value $\alpha \sim 0.01$.

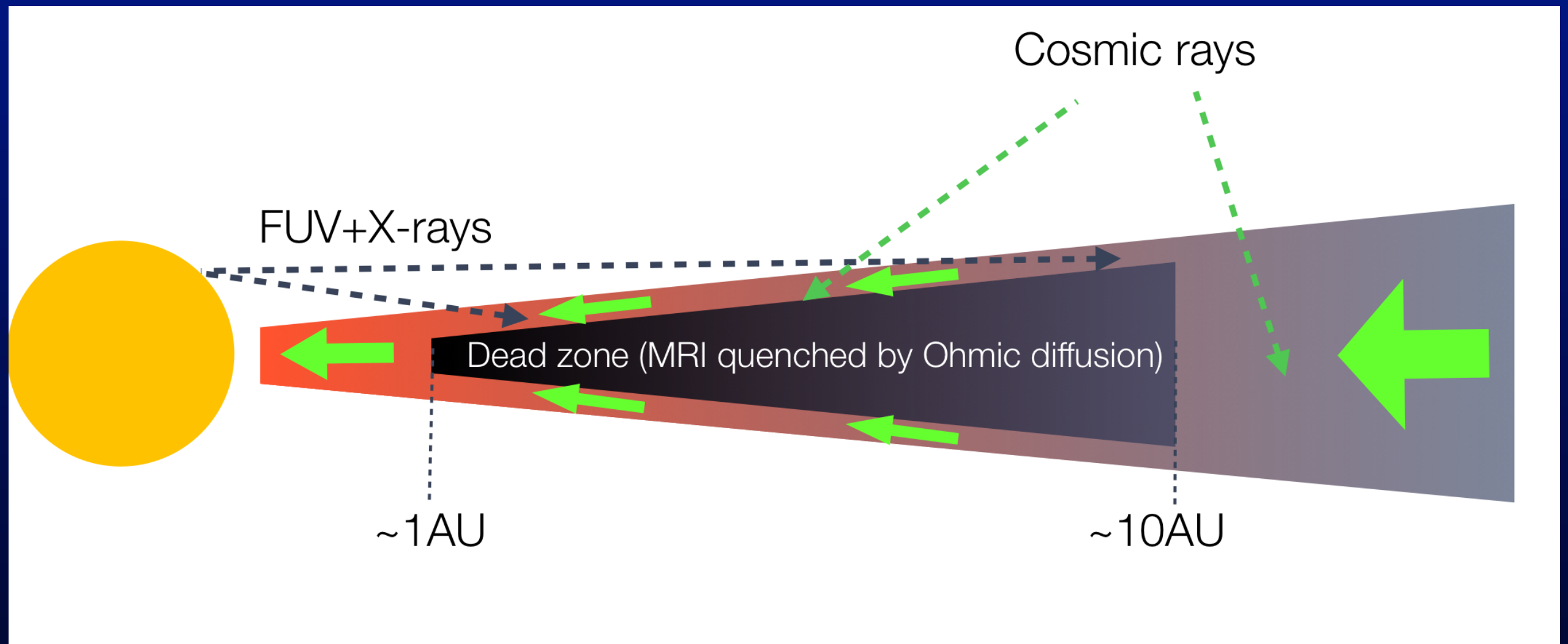


Figure from Geoffroy Lesur (PP6 talk), after Gammie (1996)

MRI requires that disc be partially ionized ($\sim 10^{-12}$). The midplane regions of protoplanetary discs may be “MRI dead”, resulting in a layered disc structure.

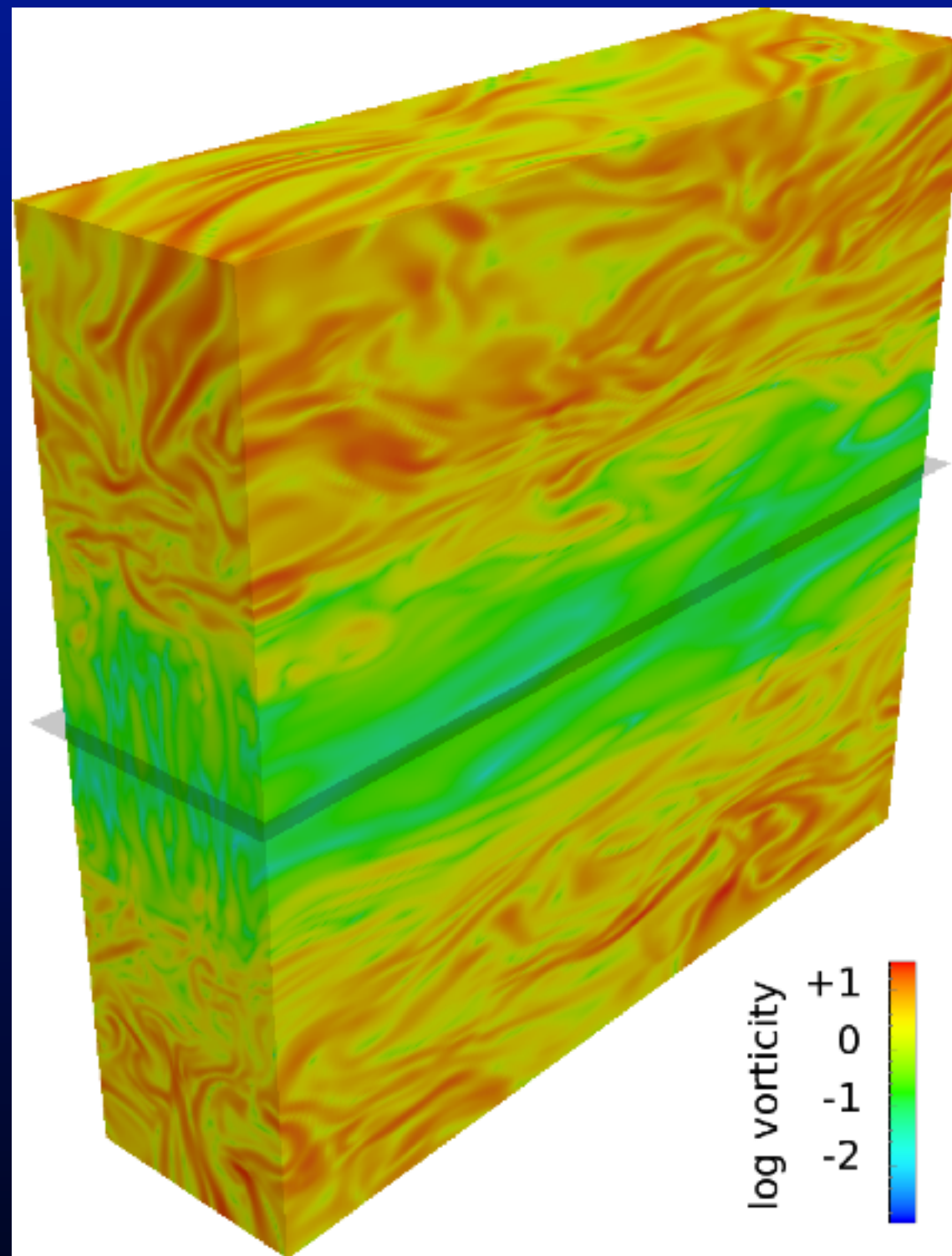


Figure from Gressel, Nelson & Turner (2011)

MRI requires that disc be partially ionized ($\sim 10^{-12}$).
The midplane regions of protoplanetary discs may be
“MRI dead”, resulting in a layered disc structure.

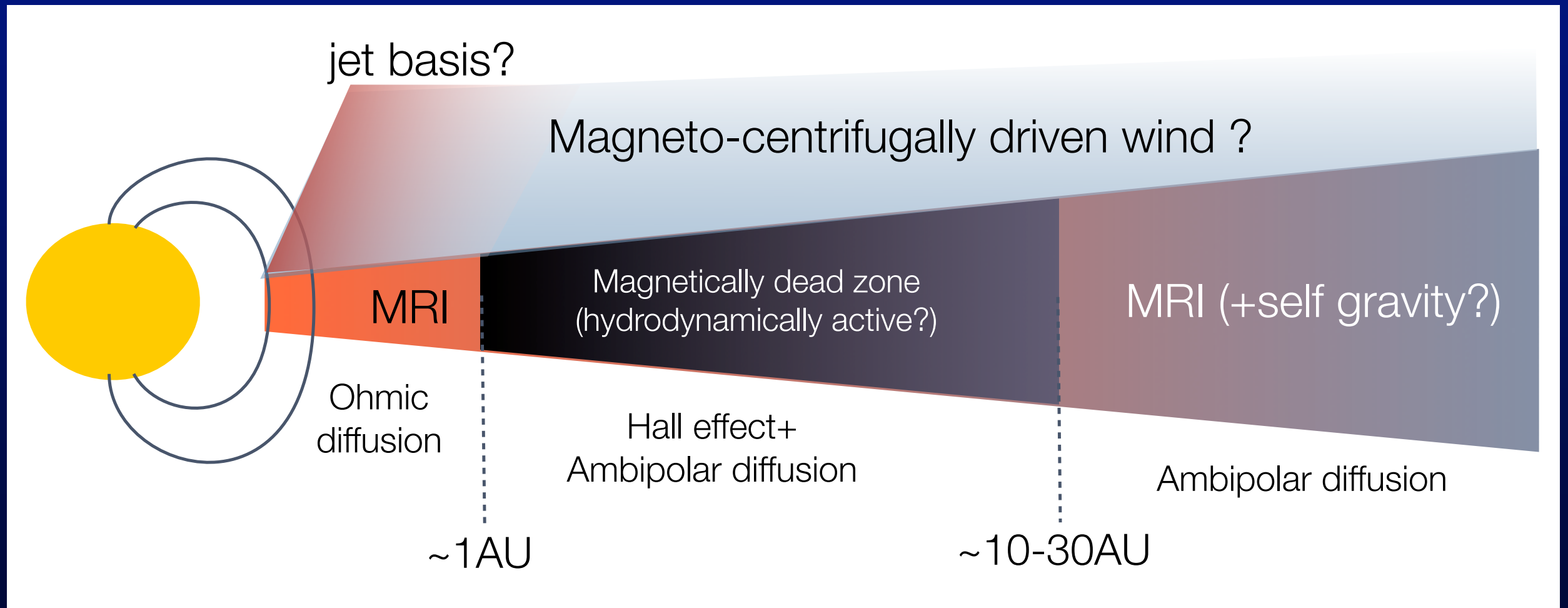
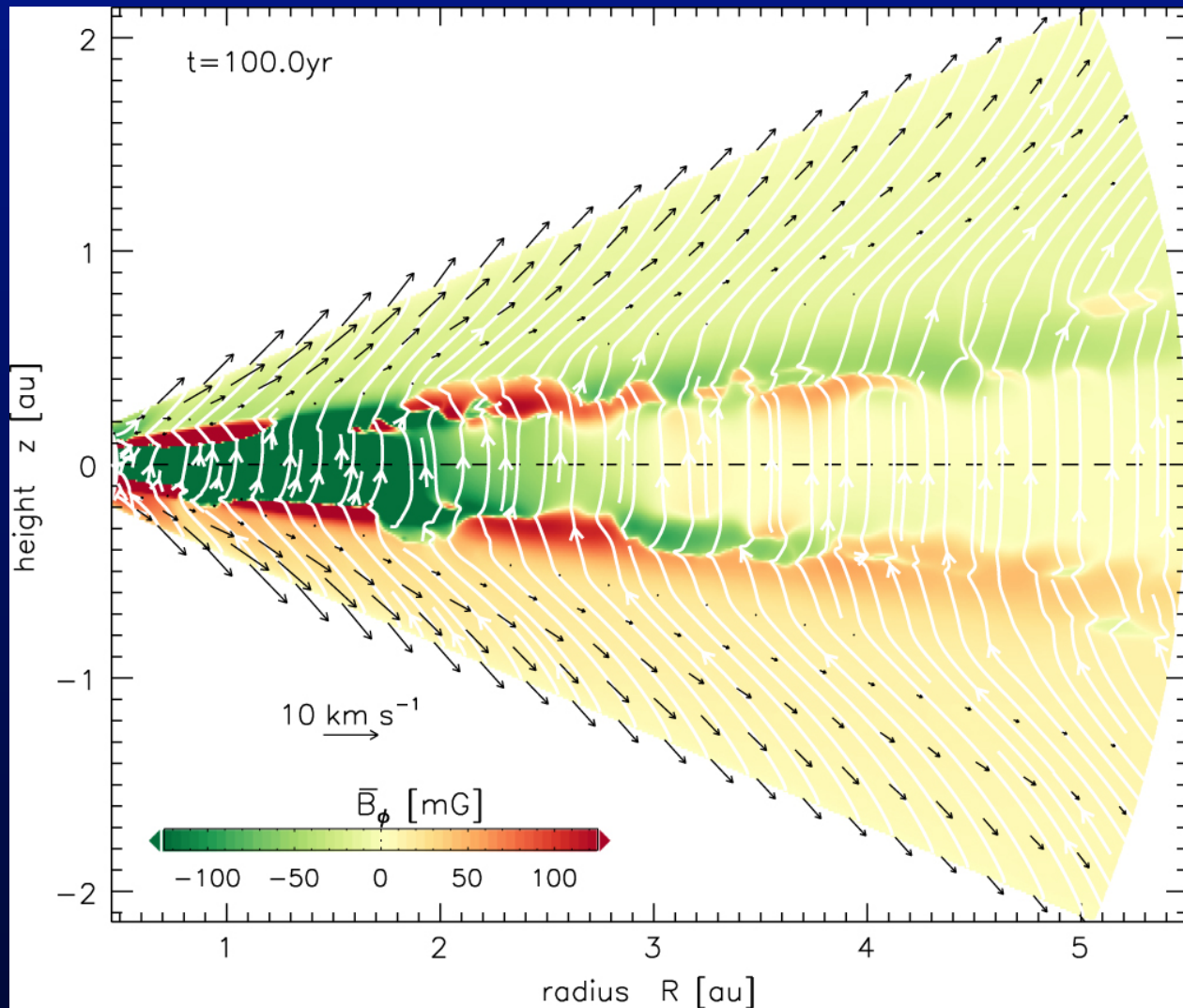
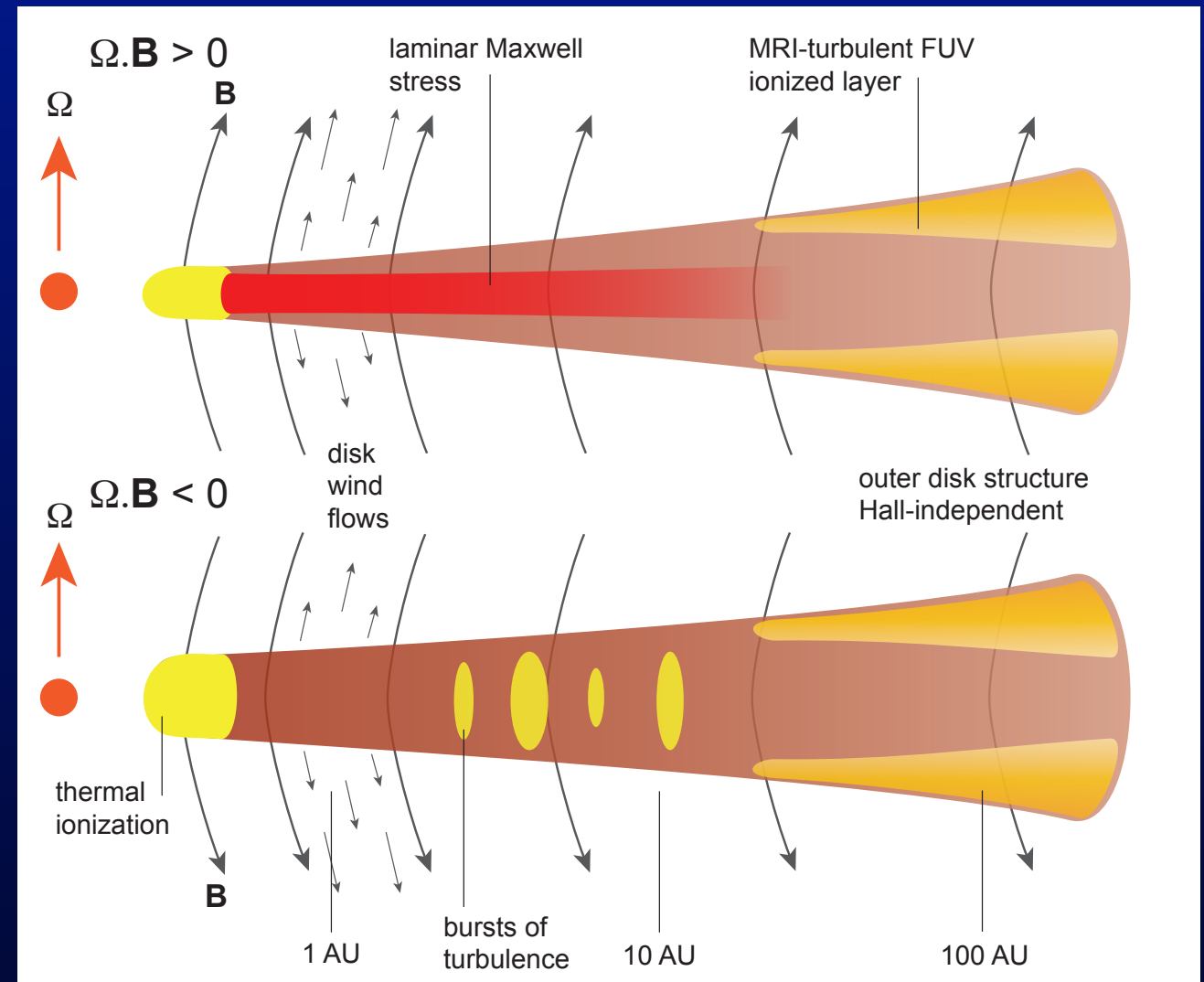


Figure courtesy of Geoffroy Lesur

In non-ideal MHD simulations, ambipolar diffusion + a vertical (poloidal) B-field invariably results in a magnetically-launched disc wind.



Gressel+ (2015)



Simon+ (2015)

Many uncertainties, remain, most notably the lack of global simulations.
 Likely that mass-loss is a combination of MRI-wind + photoevaporation: “magneto-thermal wind” (Bai+ 2016)